Surface Topography Modelling for Reduced Friction

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The aim of the present research was to investigate the possibility to design contact surfaces with reduced friction using surface roughness and topography analysis. For this purpose, different 100Cr6 plate samples with different surface topography were prepared. Using different grades and combinations of grinding and polishing samples with similar $R_a$ values, but different $R_{ku}$ and $R_{sk}$ values were prepared. To evaluate influence of roughness parameters on friction and wear, dry and lubricated pin-on-disc tests were carried out under different contact conditions. Test results show that surfaces with high $R_{ku}$ and negative $R_{sk}$ values results in reduced friction.

To investigate the effect of surface topography on surface roughness parameters and consequently on friction, real roughness profiles were virtually altered to achieve virtually textured surfaces. Using NIST SMATS softgauge for calculation of surface roughness parameters, virtually altered roughness profiles were investigated in terms of texture size, shape and spacing, and their influence on surface roughness parameters, especially on skewness and kurtosis. Lower diameter, higher spacing and wedge-shaped dimples were found to reflect in higher $R_{ku}$ and more negative $R_{sk}$ parameters, which should lead to lower friction.

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INTRODUCTION

Controlling the friction is becoming more and more important because of constant demands for improved reliability and effectiveness of mechanical parts and especially reduction in frictional loses. In recent years surface texturing was introduced as a way of reducing the friction. With employment of different patterns in form of micro dimples or groves on the surface, reduction of friction can be obtained [1] to [13]. There are some texturing parameters like shape of the dimples, their depth and width, their area density and orientation, which have influence on friction and wear. However a lot of research work was done in the field of surface texturing, modification of surface topography by texturing is still mainly based on trial and error approach.

A possible way to design surface texturing parameters, which would result in contact surfaces with lower friction, is by treating surface texturing as a controlled roughness. By knowing what kind of surface topography in terms of roughness parameters results in lower friction, we would be able to select proper surface texturing parameters. However for this knowledge about correlation between surface roughness and friction is essential.

Surface roughness and topography which are used to characterize contact surfaces are described with surface roughness parameters. Unfortunately, standard surface roughness parameters normally used by designers do not describe contact surfaces sufficiently, with completely different surfaces showing similar or even the same values of standard roughness parameters and the other way round – similar surfaces having much different standard roughness parameters. In addition to that different standards use different parameters. In practice most commonly used parameters for surface roughness description are $R_a$, $R_q$, and $R_{max}$.

Averagesurface roughness($R_a$) gives very good overall description of height variations, but does not give any information on wavelength and it is not sensitive to small changes in profile. Root mean square deviation of the assessed profile ($R_q$) is more sensitive to deviations from main line than $R_a$. However, there are also other roughness parameters defined by ISO 4287 standard, which give better surface description. $R_q$ is defined asskewness and is sensitive on occasional deep valleys or high peaks. Zero skewness reflects in symmetrical height distribution, while positive and negative skewness describe surfaces with high peaks or filled valleys, and with deep scratches or lackness of peaks, respectively. On
the other hand, kurtosis \((K_u)\) describes the probability density sharpness of the profile. For surfaces with low peaks and low valleys, \(K_u\) is less than 3, and more than 3 for surfaces with high peaks and low valleys [14]. The load bearing ratio, as well as maximum contact pressure increase with the increase of skewness and kurtosis [15]. It was also observed that parameters \(K_s, R_{pk}\) and \(R_k\) tend to have influence on coefficient of friction [16]. Parameters \(R_k, R_{pk}\) and \(R_s\) are based on the bearing ratio curve (Abbott-Firestone Curve) and are defined by the standard ISO13565-2. Core peak-to-valley height \((R_k)\) give a numerical summary of information contained in the bearing ratio curve based on a division of the curve into three regions. The upper region is defined as reduced peak height \((R_{pk})\), middle region as core region \((R_s)\) and lower region as reduced valley depth \((R_k)\). When two surfaces rub together, the peak region gets usually worn away; the core region bears the load and has influence on the life of the product and valley region which acts as a lubricant reservoir.

Therefore the aim of the present research was to investigate surface topography of contact surfaces in terms of different surface roughness parameters and to correlate surface topography changes to friction. Furthermore, to investigate the possibility of using roughness parameters as design parameters for surface topography modification, real roughness profiles were virtually altered to achieve virtually textured surfaces and roughness parameters calculated using NIST Surface Metrology Algorithm Testing System (SMATS) softgauge [17]. Virtually altered roughness profiles were investigated in terms of influence of texture size and shape on skewness and kurtosis parameters.

1. EXPERIMENTAL

For the purpose of this investigation, 100Cr6 (AISI 52100) steel samples were used. Disc type steel samples with diameter of 24 mm were prepared in terms of different average surface roughness. By using different grades of grinding and polishing results with \(R_a\) values from 0.02 to 0.49 \(\mu\)m, and different \(R_{ku}\) and \(R_k\) values were obtained. With use of different grain size and grinding parameters it is possible to obtain different surface roughness. Increasing grain size and depth of cut increased the grinding forces and surface roughness values [18].

All samples were first ground under water for 10 min, using grinding paper Piano 120, force 250N, and rotation speed of 300 rpm. Samples with average roughness \(R_a\) of about 0.5 \(\mu\)m were further grounded in water for 7 s with SiC paper and grain number 80, force 50N and rotation speed of 150 rpm. On the other hand, smoothest surfaces with a surface roughness of about 0.02 \(\mu\)m were obtained with through two step polishing. They were first polished for 10 min with 9 \(\mu\)m DP-plan disc, using force of 250N and 150 rpm, and then subsequently polished for 10 min with 6 \(\mu\)m DP-plan disc, at 200 N force and 150 rpm. To prepare surfaces with similar \(R_a\) values but different \(R_{ku}\) and \(R_k\) values, previously prepared samples with \(R_a\) values from 0.02 to 0.45 \(\mu\)m were used and treated afterwards with sandpapers or polishing pads to achieve desired roughness. Samples with higher \(R_a\) values were polished in order to remove high peaks on the surface, while polished samples were rubbed against sandpapers with different grain sizes to achieve grooves on the smooth surface. Surfacetopography of all samples was randomly orientated.

Average surface roughness \((R_a)\), root square \((R_b)\), skewness \((R_u)\), kurtosis \((K_u)\), core peak-to-valley height \((R_s)\), reduced peak height \((R_{pk})\) and reduced valley depth \((R_k)\) of prepared samples, measured on three different positions on the disc, with each incorporating 25 individual profiles, are shown in Table 1. First four surface roughness parameters are according to ISO 4287 standard, while last three parameters are according to ISO13565-2 standard. Samples tested under dry conditions are denoted with D and those under lubricated conditions as L. To investigate the influence of different roughness parameters on friction, regarding similar \(R_a\) values but different \(R_k\) and \(R_{ku}\) values, we can mutually compare samples D1 and D2 with \(R_a\) in the range of \(~0.11\mu\m\), samples D3 to D5 (\(R_a\~0.16\mu\m\)), D6 and D7 (\(R_a\~0.47\mu\m\)), L1 and L2 (\(R_a\~0.02\mu\m\)), L3 and L4 (\(R_a\~0.13\mu\m\)), L5 and L6 (\(R_a\~0.16\mu\m\)), L7 and L8 (\(R_a\~0.44\mu\m\)) (Table 1).

Tribological testing under dry and lubricated sliding conditions was carried out on Pin on disc tribometer using ball on disc contact. In order to
concentrate all the wear and surface topography changes on the investigated steel discs polished Al₂O₃ ball (Φ10 mm) was used as counterpart. Tribological testing was then performed at 3 different sliding speeds (0.05, 0.1 and 0.2 m/s) and a normal load of 1 N, which corresponds to a nominal contact pressure of 0.56 GPa. All tests (dry and lubricated) were made at a room temperature (23 ± 2 °C) and the relative humidity of 50 ± 10%, with lubricated ones carried out under boundary lubrication conditions using pure PAO 8 oil (vₐ₀ = 46 mm²/s). During testing, coefficient of friction was monitored as a function of time and wear of contact surface measured after the test by means of topography analysis.

| Table 1.Values of surface roughness parameters for different samples |
|-----------------|-------|------|--------|--------|--------|--------|
|     |  Ra   |  Rq  |  Rsk  |  Rku  |  Rk   |  Rpk  |
| D1  |  0.11 |  0.20 | -1.74 |  24.42 |  0.266 |  0.18 |  0.22 |
| D2  |  0.12 |  0.16 | -1.44 |  12.55 |  0.345 |  0.14 |  0.25 |
| D3  |  0.15 |  0.23 | -2.51 |  16.02 |  0.348 |  0.13 |  0.47 |
| D4  |  0.16 |  0.23 | -0.86 |  6.977 |  0.436 |  0.17 |  0.36 |
| D5  |  0.16 |  0.21 | -0.38 |  4.240 |  0.488 |  0.18 |  0.27 |
| D6  |  0.49 |  0.74 | -1.33 |  10.80 |  1.360 |  0.81 |  1.44 |
| D7  |  0.45 |  0.59 | -0.90 |  5.341 |  1.334 |  0.40 |  0.88 |
| L1  |  0.02 |  0.02 |  0.25 |  3.075 |  0.071 |  0.02 |  0.01 |
| L2  |  0.04 |  0.05 | -1.37 |  16.63 |  0.132 |  0.03 |  0.05 |
| L3  |  0.12 |  0.17 | -0.27 |  9.310 |  0.352 |  0.07 |  0.26 |
| L4  |  0.13 |  0.19 | -1.67 |  12.21 |  0.304 |  0.18 |  0.32 |
| L5  |  0.16 |  0.21 | -0.38 |  4.240 |  0.488 |  0.17 |  0.27 |
| L6  |  0.16 |  0.26 | -3.11 |  23.20 |  0.342 |  0.17 |  0.53 |
| L7  |  0.44 |  0.6  | -1.32 |  10.29 |  1.002 |  0.65 |  1.41 |
| L8  |  0.45 |  0.59 | -0.90 |  5.341 |  1.334 |  0.40 |  0.88 |

3. RESULTS AND DISCUSSION

3.1 Dry Sliding

For all tests, made under dry sliding conditions, combination of plastic deformation and abrasion was found as main wear mechanism (Fig. 1a), resulting in complete change in surface topography. Consequently wear volume and sliding distance, when steady state friction conditions are reached displayed very high degree of scattering, as shown in Table 2.

However, when comparing samples D1 and D2, with sample D1 having much higher Rₖᵤ value at similar average roughness, coefficient of friction tends to be lower for sample D1. Comparison of samples D3, D4 and D5 which have similar Rₙ and Rₖ values, but different Rₖₙ and Rₖᵤ, shows that surface with the lowest skewness and the highest kurtosis (D3) also results in the lowest friction. Furthermore for sample D3 friction is almost independent of the sliding speed, while for samples D4 and D5 friction is reduced with increase in sliding speed. Also the sliding distance to steady-state conditions is the shortest for sample D3, which is true for all sliding speeds.

| Table 2.Coefficient of friction and sliding distance to steady state conditions for dry sliding |
|-----------------|---|---|---|---|---|---|---|---|---|
| Coefficient of friction | 0.05 | 0.1 | 0.2 | 0.05 | 0.1 | 0.2 |
| 0.05 | m/s | m/s | m/s | m/s | m/s | m/s |
| D1 | 0.89 | 0.92 | 0.91 | 34 | 50 | 38 |
| D2 | 0.96 | 0.93 | 0.93 | 49 | 28 | 38 |
| D3 | 0.89 | 0.90 | 0.89 | 31 | 29 | 16 |
| D4 | 0.94 | 0.89 | 0.86 | 37 | 39 | 30 |
| D5 | 0.99 | 0.97 | 0.92 | 39 | 30 | 33 |
| D6 | 0.82 | 0.85 | 0.87 | 35 | 39 | 42 |
| D7 | 0.84 | 0.63 | 0.66 | 40 | 24 | 34 |

When comparing samples D6 and D7, which have the highest Rₙ and Rₖ values between all D samples, lower friction and shortest sliding distance to steady state condition were obtained for sample D7, which displays smaller values of Rₖₙ and Rₖᵤ parameters. For sample D6 sliding speed has very minor effect on friction, while for sample D7 increase in sliding speed results in reduced friction.

However, experimental results show that for dry sliding in general coefficient of friction is lower when roughness is low, and it gets reduced...
with increase in sliding speed. Furthermore, for surfaces with high value of $R_{ku}$ and more negative $R_{sk}$ parameter, friction also tends to be lower.

Under dry sliding high degree of wear and change in surface topography limits proper comparison and correlation between surface roughness and tribological properties of contact surfaces.

3.2 Lubricated Sliding

Under lubricated sliding original topography of the contact surfaces was preserved during the test (Fig. 1b), with higher sliding speed generally resulting in lower friction. Coefficient of friction and sliding distance to steady state conditions for lubricated testing are summarized in Table 3.

Table 3. Coefficient of friction and sliding distance to steady state conditions for lubricated sliding

<table>
<thead>
<tr>
<th>Coefficient of friction</th>
<th>Sliding distance to steady state conditions</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>0.05</td>
</tr>
<tr>
<td>L1</td>
<td>0.11</td>
</tr>
<tr>
<td>L2</td>
<td>0.09</td>
</tr>
<tr>
<td>L3</td>
<td>0.14</td>
</tr>
<tr>
<td>L4</td>
<td>0.14</td>
</tr>
<tr>
<td>L5</td>
<td>0.15</td>
</tr>
<tr>
<td>L6</td>
<td>0.10</td>
</tr>
<tr>
<td>L7</td>
<td>0.14</td>
</tr>
<tr>
<td>L8</td>
<td>0.16</td>
</tr>
</tbody>
</table>

In the case of smooth surfaces (samples L1 and L2), sample L2 gave lower friction although its average roughness ($R_a$) was higher than for L1. However, while sample L1 has positive skewness and kurtosis around 3, L2 has negative skewness and very high kurtosis. Beside lower friction sample L2 also shows reduction in sliding distance to steady-state conditions with sliding speed as compared to sample L1 where it increases as shown in Table 3. For samples with $R_a$ values around 0.12 μm (L3 and L4) similar friction was observed although L4 displays higher $R_{ku}$ value and more negative $R_{sk}$ than sample L3. On the other hand, difference in $R_{sk}$ and $R_{ku}$ roughness parameters has an influence on sliding distance when steady state conditions are reached. Sample L4 with higher $R_{ku}$ and more negative $R_{sk}$ shows drastically shorter sliding distances, as shown in Table 3.

When comparing samples with $R_a$ values of about 0.16 μm (L5 and L6), effect of parameter $R_{ku}$ and $R_{sk}$ is even more pronounced. Higher $R_{ku}$ and more negative $R_{sk}$ values measured for sample L6 result in lower friction. Furthermore, when comparing coefficient of friction for sample L6 and samples L3 and L4, it can be seen, that sample L6 shows lower friction and shorter sliding distance to steady state conditions although displaying higher $R_a$ values. In the case of the roughest samples (L7 and L8), with $R_a$ values ~0.45 μm, similar tendencies were observed, with higher $R_{ku}$ and more negative $R_{sk}$ values leading to lower friction. On the other hand, for very rough surfaces sliding distance to steady state condition tends to increase with increase in $R_{sk}$ and $R_{ku}$ parameters (L7).

Interesting results were observed when comparing samples L3 and L7. Although sample L7 shows much higher average surface roughness, it has similar $R_{sk}$ and $R_{ku}$ value and consequently gives similar friction under lubricated sliding. However, as expected sliding distance to steady state condition is shorter for smoother surface (sample L3).

It can be also noticed that all samples which resulted in lower friction (L2, L4, L6 and L7) show lower values of $R_{sk}$ regarding to the mutually compared samples (Table 1).

Taking a look at the nature of surface roughness parameters $R_{ku}$ and $R_{sk}$, it can be seen that negative $R_{sk}$ describes surfaces with deep scratches or lackness of peaks, and parameter $R_{ku}$ greater than 3, surfaces with high peaks and low valleys. By combining those two descriptions, we end up with smooth surface containing deep valleys. If we treat surface texturing as ordered roughness, those deep valleys can be treated as micro-dimples. With implementation of micro dimples we get more ordered surface which should reflect in lower friction. Main idea of surface texturing is that textures act either as micro-traps for capturing wear debris or as micro-reservoirs which enhance lubrication. When comparing experimental results with idea of surface texturing some correlations can be observed. Under dry sliding higher values of parameter $R_{ku}$ and more negative values of parameter $R_{sk}$ led to lower friction, indicating that deep valleys act as wear particle traps. The same
tendency was observed under lubricated sliding, where greater $R_{ku}$ and more negative $R_{sk}$ values give lower friction and shorten sliding distance to steady-state condition. In this case it can be assume that deep valleys act as micro reservoirs, which enhance lubrication. Accordingly a general conclusion can be drawn, that $R_{ku}$ and $R_{sk}$ have an influence on friction and therefore could be used as a guideline for designing surface topography with reduced friction.

4. MODELLING

To investigate the effect of surface texturing on surface roughness parameters and to analyse the possibility of using roughness parameters for designing contact surfaces, real roughness profile was virtually altered to achieve virtually textured surfaces. Using NIST SMATS [17] softgauge for calculation of surface roughness parameters, virtually altered roughness profiles were investigated in terms of effect of texture size and shape on surface roughness parameters, especially on skewness and kurtosis.

Real roughness profile was obtained using stylus profilometer. Polished sample with $R_a$ value of 0.02 $\mu$m ($R_q = 0.024 \mu$m, $R_{sk} = 0.24$, $R_{ku} = 3.07$) was used as the origin profile. This profile was then virtually altered using Microsoft Excel to achieve virtually textured surfaces as shown in Fig. 2 and influence of different spacing, and dimple diameter, shape and depth on the surface roughness parameters investigated. According to experimental results which emphasized $R_{ku}$ and $R_{sk}$ as the most influencing parameters, modelling was concentrated on finding texturing parameters, which would reflect in high $R_{ku}$ and more negative $R_{sk}$ values.

First the effect of spacing between dimples was investigated. Rectangular dimples with a diameter of 0.12 $\mu$m and depth of 6 $\mu$m were simulated by shifting down the original profile for the value of the dimple depth. This surface topography modelling showed that increase in spacing result in decreased $R_a$, $R_q$ and $R_{sk}$ values and increased $R_{ku}$ value. For instance, if spacing is increased from 0.12 mm to 0.24 mm, $R_{sk}$ will decrease and $R_{ku}$ increase from -0.668 to -1.026, and from 1.492 to 3.028, respectively. With further increase in spacing between dimples, $R_a$ and $R_q$ values are further decreased and $R_{ku}$ further increased. However, for $R_{sk}$ parameter increase in spacing between dimples after initial reduction leads to increase in $R_{sk}$ value, as shown in Fig. 3.

Varying the depth of dimples was found to have very minor effect on the $R_{sk}$ and $R_{ku}$ parameter values. For the same diameter of 0.12 mm, changing the depth from 6 to 10 $\mu$m resulted in doubled $R_a$ and $R_q$ values, but almost equal values of $R_{sk}$ and $R_{ku}$ parameter. The same observations were found for smaller dimple diameters and larger dimple depths. Changing the diameter of dimples only slightly affects $R_a$, $R_q$ and $R_{ku}$ parameters but has a considerable effect on $R_{sk}$ value. Reduction in dimple diameter results in only minor increase in $R_q$, $R_{sk}$ and $R_{ku}$ values but drastic increase in $R_{sk}$, as shown in Fig. 4.

![Fig. 2. Example of virtually textured surface (diameter of dimples 0.06 mm, spacing 0.24 mm, depth 6$\mu$m, rectangular shape)](image)

![Fig. 3. Surface roughness parameters in dependence of spacing between dimples (diameter of dimples 0.12 mm, depth 6$\mu$m)](image)
Fig. 4. Surface roughness parameters in dependence of diameter of the dimples (spacing 0.12 mm, depth 6 μm)

Finally, the shape of the dimples was investigated, using dimples with a diameter of 0.12 mm and spacing of 0.12 mm. By changing the slope of the dimple walls (Fig. 5a), increase in slope angle was found to result in reduced values of $R_a$, $R_q$ and $R_{sk}$ parameters in increased values of $R_{ku}$. By shifting the bottom of the dimple to one side ($\alpha \neq \beta$, Fig. 5b) higher values of $R_{ku}$ and more negative $R_{sk}$ are obtained, as shown in Table 4. Such dimple shapes should also have good hydrodynamic effects. As can be seen from Table 4, the most suitable values of $R_{ku}$ and $R_{sk}$ parameter are obtained when angle $\alpha$ is close to 90° and $\beta$ is very small, but not 0°.

By combining different dimple parameters, such as bigger spacing between dimples (0.36 mm), smaller diameter (60 μm) and wedge-shaped dimple ($\alpha = 82.4^\circ$ and $\beta = 24.7^\circ$), for which it has been found to increase $R_{ku}$ and decrease $R_{sk}$ values, very high values of $R_{ku}$ (12.3) and negative $R_{sk}$ (-2.7) can be obtained. Additionally, such texturing parameters also result in lower $R_a$ and $R_q$ values (0.44 and 0.92 μm, respectively). According to the experimental results, presented in this paper, such shape and spacing of the dimple should result in lower friction. However, these findings still need to be experimentally confirmed.

Table 4. Roughness parameters vs. dimples wall angle (diameter 0.12 mm, depth 6 μm)

<table>
<thead>
<tr>
<th>$\alpha$ and $\beta$</th>
<th>$R_a$</th>
<th>$R_q$</th>
<th>$R_{ku}$</th>
<th>$R_{sk}$</th>
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<tbody>
<tr>
<td>$\alpha = \beta = 0^\circ$</td>
<td>1.85</td>
<td>1.93</td>
<td>1.35</td>
<td>0.03</td>
</tr>
<tr>
<td>$\alpha = 0^\circ$, $\beta = 59^\circ$</td>
<td>1.18</td>
<td>1.69</td>
<td>2.25</td>
<td>-0.04</td>
</tr>
<tr>
<td>$\alpha = 0^\circ$, $\beta = 75^\circ$</td>
<td>1.56</td>
<td>1.67</td>
<td>1.42</td>
<td>-0.26</td>
</tr>
<tr>
<td>$\alpha = 0^\circ$, $\beta = 83.7^\circ$</td>
<td>1.07</td>
<td>1.31</td>
<td>2.96</td>
<td>-1.05</td>
</tr>
<tr>
<td>$\alpha = 85.4^\circ$, $\beta = 14.6^\circ$</td>
<td>1.21</td>
<td>1.45</td>
<td>2.55</td>
<td>-0.86</td>
</tr>
<tr>
<td>$\alpha = 86.2^\circ$, $\beta = 14.6^\circ$</td>
<td>1.07</td>
<td>1.33</td>
<td>3.21</td>
<td>-1.05</td>
</tr>
<tr>
<td>$\alpha = 83.7^\circ$, $\beta = 0^\circ$</td>
<td>1.52</td>
<td>1.69</td>
<td>0.33</td>
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<td>$\alpha = 86.3^\circ$, $\beta = 0^\circ$</td>
<td>1.29</td>
<td>1.56</td>
<td>2.61</td>
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<tr>
<td>$\alpha = 86.9^\circ$, $\beta = 0^\circ$</td>
<td>1.14</td>
<td>1.44</td>
<td>3.30</td>
<td>-0.99</td>
</tr>
</tbody>
</table>

5 CONCLUSIONS

Under dry sliding high wear rates and change in surface topography blurs the effect of surface roughness on friction. However, in general lower roughness of the contact surface and higher sliding speeds result in lower friction, with surfaces displaying higher kurtosis ($R_{ku}$) values and more negative skewness ($R_{sk}$) parameter often having an advantage.

For lubricated sliding contact kurtosis and skewness were found to be the most important roughness parameters in terms of tribological behaviour. Use of surfaces with
higher kurtosis and more negative skewness always reflects in lower friction and shorter distance when steady-state condition was reached, even if average roughness is not the same. Plateau-like topography of contact surfaces with high kurtosis and more negative skewness and effect of kurtosis and skewness on friction indicate that these parameters could be used as design parameters for surface topography modification and texturing aimed to reduce friction.

By surface topography modelling, surface texturing parameters which would result in greater kurtosis and more negative skewness parameter and consequently in lower friction in boundary lubrication can be defined. These parameters are lower diameter of the dimple, higher spacing between the dimples and wedge-like shape of the dimples.

5. REFERENCES


