INTRODUCTION

Drilling is an essential part of processes used in subtractive manufacturing for achieving the desired products. Its massive usage requires that any parameter optimization in the process promotes the efficiency and the greener machining. Cutting tool technology is considered one of the most significant impact factors on the sustainability of machining processes and systems. Therefore, the best choice of cutting tools and parameters for the quality of the products and the tool life criterion are both critical for the sustainability metrics of a drilling process. The correct usage of the cutting tool can affect the reduction of needed resources and energy for the production of a new one. Aluminium alloy 7075 (Al7075) is suitable for a variety of specific applications in the aerospace and chemical industries because of its excellent mechanical properties. Its strength, which is comparable to many steels and its excellent corrosion resistance are the main reasons that researchers focus on it [1] to [3]. The chemical composition of Al7075 is given in Table 1.

The development of an appropriate cutting factor analytical model is challenging. Nevertheless, there is much research developed about the suitability of different empirical models to predict different factors during several cutting processes. A number of methods, such as artificial neural networks (ANN) and response surface methodology (RSM), have been developed for modelling many manufacturing parameters. The successful application of ANN for prediction and modelling purposes in several science and engineering domains is substantial. ANN is utilized for modelling and prediction purposes due to its advantages in non-linear response and when time variability occurs. It covers the difficulty in inferring input/output mapping [4] and [5] and the search algorithms for optimization, based on genetic and evolution principles [6] to [8]. RSM is a reliable statistical tool for the mathematical modelling of engineering systems and for the optimization of different manufacturing processes.

Table 1. Chemical composition of Al7075

<table>
<thead>
<tr>
<th>Elements</th>
<th>Zn</th>
<th>Mg</th>
<th>Cu</th>
<th>Cr</th>
<th>Fe</th>
<th>Si</th>
<th>Mn</th>
<th>Ti</th>
<th>Al</th>
</tr>
</thead>
<tbody>
<tr>
<td>Percentage</td>
<td>6</td>
<td>3</td>
<td>2</td>
<td>0.3</td>
<td>0.6</td>
<td>0.5</td>
<td>0.4</td>
<td>0.3</td>
<td>Balance</td>
</tr>
</tbody>
</table>
It has been considered to be useful with minimum knowledge about the process under consideration, while simultaneously reducing the resources needed for experiments. It is an appropriate methodology when many factors and interactions affect the desired responses for a given process and an effective technique for evaluating the process parameters with the least number of experiments [9] to [12].

The present paper deals with the study of the drilling process of Al7075 when using solid carbide tools. A series of different diameters were used, together with a number of different cutting speeds and feed rates. A complete set of experimental work was implemented, and different mathematical models of the thrust force and torque developed were calculated. Both RSM and ANN methodologies were applied, and although their results were highly accurate, the ANN model was more effective.

1 METHODS

As mentioned before, a number of researchers have focused on the development of empirical models to predict different factors during several cutting processes. Nouioua et al. [13] developed ANN and RSM models related to cutting force and surface roughness during the turning process of X210Cr12 steel under dry, wet, and MQL machining. Multilayer-coated tungsten carbide inserts with various nose radii were used for the experiment. Measurements were taken combining cutting speed, feed rate, and cutting depth. The comparison between ANN and RSM models showed that ANN models are more accurate for the prediction of surface roughness and cutting force. Kumar and Chauhan [14] used RSM and ANN methodologies in turning, for the validation of the results obtained during experimentation and the prediction of the behaviour of the system under any condition within the operating range. Al7075 hard ceramic composite and Al7075 hybrid composite were under investigation according to the effect of cutting parameters (cutting speed, feed rate, and approach angle) on roughness, using a polycrystalline diamond tool (PCD).

Furthermore, RSM, ANN and support vector regression (SVR) in turning operations were used [15] for the development of empirical models for predicting surface roughness, tool wear, and power required. These response parameters were mainly dependent upon cutting velocity, feed, and cutting time. The result was that ANN and SVR models are much better than RSM models for predicting the three response parameters. ANN and multiple regression approaches were also used for the measurement of the surface roughness of AISI 1040 steel during turning at different cutting parameters, including speed, feed, and depth of cut [16]. The full factorial experimental design was implemented to increase the confidence limit and reliability of the experimental data. Finally, it was proved that the ANN model estimated the surface roughness more accurately than the multiple regression model did.

Many researchers have investigated the appropriateness of different empirical models to predict burr size during drilling. Karnik et al. [17] described the comparison of the burr size predictive models based on ANN and RSM on AISI 316L stainless steel workpiece with cutting speed, feed and point angle as the critical parameters. The comparison showed that the ANN models provide more accurate predictions than the RSM models do. The result was the same for Çiçek et al. [18] for the investigation of the effects of cutting parameters (i.e. cutting speed, feed rate) and deep cryogenic treatment on thrust force in the drilling of AISI 316 stainless steel. Using the same techniques Mayyas et al. [19] investigated the influence of cutting speed, feed and volume fraction of the reinforcement particles used on the thrust force and torque in the drilling processes of self-lubricated hybrid composite materials. While Bajić et al. [20] examined the influence of three cutting parameters (cutting speed, feed per tooth and depth of cut) on surface roughness, tool wear and cutting force components in a face milling as part of the off-line process control. Alharthi et al. [21] developed ANN and regression analysis models for the prediction of surface roughness in a face milling of an AZ61 magnesium alloy workpiece, for different spindle speed [rpm], depth of cut [mm], and table feed [mm/ min]. The coefficient of determination was found to be sufficiently accurate for the best neural network and regression analysis model from the comparison of the models with thirteen experimental validation tests.

Rooki et al. [22] described a simple and more reliable ANN method and multiple linear regressions (MLR) for the prediction of cutting concentration during foam drilling operation. The results indicated the high ability in the prediction of ANN methods. Kahraman [23] investigated the predictability of penetration rate for the diamond drilling from the operational variables and the rock properties, such as the uniaxial compressive strength, the tensile strength and the relative abrasiveness. Finally, Chavoshi [24] using methods, such as regression analysis (RA), ANN, and co-active neuro-fuzzy inference system (CANFIS) attempted to predict the surface roughness,
material removal rate, and over-cut of SAE-XEV-F valve-steel during electrochemical drilling in NaCl and NaNo3 electrolytic processes.

2 EXPERIMENTAL

2.1 Experimental Settings

In this study, an Al7075 plate was used as the workpiece material (150 mm × 150 mm × 15 mm). The drilling tests were performed using a HAAS VF1 CNC machining centre with continuous speed and feed control within their boundaries. The cutting forces were measured by utilizing a Kistler four components dynamometer (type 9123) with all the appropriate accessories. The dynamometer signals were processed via charge amplifiers and an A/D converter to a personal computer. The measured thrust force and torque were displayed and analysed to implement an early error detection strategy.

During the drilling tests, thrust force \( F_z \) and torque \( M_z \) values were measured in 36 experiments which were performed by using solid carbide drill tools (Kennametal - multilayer TiAlN-PVD-coated universal fine-grain grade). Fig. 1 shows details of the cutting tool geometry.

![Cutting tool geometry](image)

Fig. 1. Cutting tool; a) geometry details; and b) dimensions

The cutting tools are not through coolant category tools; therefore, coolant fluid (90% water,
10 % KOOLRite 2270 coolant) was provided by the delivery system near the cutting tool. The feed rates of 0.2 mm/rev, 0.4 mm/rev, and 0.6 mm/rev were used together with cutting velocity values of 10 m/min, 40 m/min, and 70 m/min. The constant depth of the holes drilled was 15 mm. The full factorial set of tests was performed for all the combinations of cutting speeds, feed rates, and tool diameters. The workflow of the research is depicted in Fig. 2 and the cutting parameters, units, and notations are listed in Table 2.

Table 2. Cutting variables used in the experiments

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Values</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cutting velocity, $V$ [m/min]</td>
<td>10, 40, 70</td>
</tr>
<tr>
<td>Feed rate, $f$ [mm/rev]</td>
<td>0.2, 0.4, 0.6</td>
</tr>
<tr>
<td>Tool diameter, $D$ [mm]</td>
<td>8, 10, 12, 14</td>
</tr>
<tr>
<td>Axial depth of cut, $d_c$ [mm]</td>
<td>15</td>
</tr>
<tr>
<td>Workpiece dimension [mm]</td>
<td>150 × 150 × 15</td>
</tr>
</tbody>
</table>

Fig. 3 expresses the evolution of thrust force and the cutting torque related to different feed rates and cutting speeds. According to the graph, it can be seen that when the tool diameter increases, both the thrust force and the cutting torque values are increased as expected. The same happens in the case of the feed rate. As feed rate values are increased, the thrust force and the cutting torque are then increased respectively. In contrast, the different values of cutting speed do not noticeably affect the experimental values. The importance of cutting tool diameter and feed rate is much greater than that of cutting speed related to thrust force and cutting torque.

2.2 RSM-Based Predictive Models

The RSM is an accurate tool used to check the influence of a series of input variables on the response when studying a complex phenomenon. The models produced use the least square fitting in order to provide a reliable mathematical model. In this case, a full factorial strategy was followed, 36 drilling experiments were performed, and both the thrust force and torque were modelled using polynomial
mathematical models. The following form was selected for this case:

\[
Y = b_0 + b_1 X_1 + b_2 X_2 + b_3 X_3 + b_4 X_4 + b_{11} X_2^2 + b_{22} X_3^2 + b_{33} X_4^2 + b_{44} X_2^2 + b_{12} X_1 X_2 + b_{13} X_1 X_3 + b_{14} X_1 X_4 + b_{23} X_2 X_3 + b_{24} X_2 X_4 + b_{34} X_3 X_4,
\]

where \( Y \) is the response, \( X_i \) stands for the coded values and \( b_{00}, \ldots, b_{34} \) stand for the models’ regression coefficients.

Based on this mathematical model, the data acquired formed the following equations for the thrust forces [N] and the torque [Nm] respectively:

\[
F_z = -166 + 43.2 D + 0.405 V + 1273 f + 2.10 D \times D + 0.0163 V^2 + 86 f^2 - 0.140 D \times V + 64.2 D \times f + 0.156 V \times f
\]

and

\[
M_z = 4.52 - 0.913 D - 0.00502 V - 7.31 f + 0.0548 D \times D - 0.000046 V^2 - 1.39 f^2 + 0.000405 D \times V + 1.73 D \times f + 0.0197 V \times f
\]

where \( D \) is the tool diameter [mm], \( f \) is the feed rate [mm/rev], and \( V \) is the cutting speed used [m/min] and solid carbide tools and Al7075 workpiece.

The adequacy of the models is provided at a 5 % level of significance. ANOVA was used for establishing the validity of the developed models. The calculated values of the F-ratio of the developed models (Tables 3 and 4), are significantly increased compared to the tabulated value of the F-table at a 95 % confidence level (2212.84 for the \( F_z \) and 2908.77 for the \( M_z \)), while the \( P \)-values are 0.000, which proves the highest correlation between data and model in each case. The validity of the models is also proved because the R-sq(adj) is very high in both cases (99.8 % for the \( F_z \) and 99.9 % for the \( M_z \)). In addition, the significant terms of the models, when a level of significance of 5 % is used, are those with a \( P \)-value less than 0.05. For the \( F_z \) these factors are: \( D (P = 0.016), f (P = 0.000), D \times D (P = 0.008), V \times V (P = 0.015) \) and \( D \times f (P = 0.000) \), while for the \( M_z \) the significant terms are: \( D (P = 0.000), f (P = 0.000), D^2 (P = 0.000), D \times f (P = 0.000), V \times f (P = 0.000) \).

Residual analysis was performed to test the models’ accuracy; in both cases, the residuals follow the normal distribution. They follow straight lines (almost linear patterns) proving that the errors follow the normal distribution. All the scatter diagrams of the \( F_z \) and \( M_z \) residuals versus the fitted values depict that the residuals are evenly distributed on both sides of the centreline.

The same is true for the residuals versus the order of the data (see Fig. 4). The accuracy achieved is very high when comparing the measured values and those calculated from the mathematical models (3 % and 5.6 %, respectively). The derived mathematical models can be considered to be very accurate and can be used directly for predicting both the thrust force and the cutting torque within the limits of the tool diameter, feed rate, and cutting speed used.

### Table 3. ANOVA table for the \( F_z \) (thrust force)

<table>
<thead>
<tr>
<th>Source</th>
<th>DF</th>
<th>SS</th>
<th>MS</th>
<th>F</th>
<th>P</th>
</tr>
</thead>
<tbody>
<tr>
<td>Regression</td>
<td>9</td>
<td>6239800</td>
<td>693311</td>
<td>2212.84</td>
<td>0.000</td>
</tr>
<tr>
<td>Residual Error</td>
<td>26</td>
<td>8146</td>
<td>313</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Total</td>
<td>35</td>
<td>6247946</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

R-Sq(adj) = 99.8 %

### Table 4. ANOVA table for the \( M_z \) (torque)

<table>
<thead>
<tr>
<th>Source</th>
<th>DF</th>
<th>SS</th>
<th>MS</th>
<th>F</th>
<th>P</th>
</tr>
</thead>
<tbody>
<tr>
<td>Regression</td>
<td>9</td>
<td>322187</td>
<td>35799</td>
<td>2908.77</td>
<td>0.000</td>
</tr>
<tr>
<td>Residual Error</td>
<td>26</td>
<td>0.320</td>
<td>0.012</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Total</td>
<td>35</td>
<td>322507</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

R-Sq(adj) = 99.9 %
Fig. 4. Residual analyses for the Fz and Mz a) Normal Probability Plot of the Residuals, b) Residuals Versus the Fitted Values, c) Residuals Versus the Order of the Data

Fig. 5. Architecture of ANN with a) 3 inputs-6 to 12 hidden neurons -2 outputs, and b) 3 inputs-6 to 12 hidden neurons -1 output topology
2.3 ANN Modelling

Artificial Neural Network ability to learn complex non-linear and multivariable relationships between process parameters makes them very useful in many applications. An ANN consists of a number of neurons, which are divided into the three basic layers: input, hidden, and output. The neurons between the layers are linked, having synaptic weights. One of the basic advantages of ANN is its ability to learn from the process. When the architecture of the network is defined, then, through a learning process, weights are calculated to present the desired output.

The present research used a series of neural network pieces of software available for the development of a multilayer feedforward neural network. An elementary neuron with \( R \) inputs is shown in Figure 6a. Each input is weighted with an appropriate value \( w \). The sum of the weighted inputs and the bias forms the input to the transfer function \( f \). Neurons can use any differentiable transfer function \( f \) to generate their output.

The standard network that is used for function fitting is a two-layer feedforward network, with a tan-sigmoid transfer function in the hidden layer and a linear transfer function in the output layer (see Fig. 6b). Assuming that the activation function used in the hidden and the outer layer is sigmoidal, the outputs of the hidden and outer layer were calculated using the following equation:

\[
 f(\text{net}) = \frac{1}{1 + e^{-\text{net}}}. 
\]  

Fig. 6. Multilayer neuron network architecture, a) elementary neuron with \( R \) inputs, b) linear transfer function

All of the original (36) experimental data were randomly divided into three data sets including training, validation and testing. The back-propagation training algorithms, the scaled conjugate gradient (SCG) and Levenberg–Marquardt (LM), were used for ANNs training. The training set used 70% of the data to build the network, 15% to measure network generalization and 15% as a testing set of the neural network. Three-layer network architectures were used to predict the thrust force and torque as shown in Fig. 5.

In the first case, a 3-(6-12)-2 ANN topology was used, which consists of three input nodes (tool
diameter, cutting speed, feed rate), one hidden layer (6 to 12 neurons) and two outputs (thrust force and torque). In the second case, two different 3-(6–12)-1 ANN topologies were used as the output layer consists of one neuron corresponding to one output variable $F_z$ and $M_z$, respectively.

In consequence of trials, the best network architecture for the prediction of thrust force was the 3-10-1 topology. The comparison of predicted results from ANN model with experimental measurements shows that there is a very good correlation between them. It is obvious that a neural network is an excellent tool for predicted values of $F_z$ according to experimentally measured ones. The correlation coefficient ($R$ value) between the outputs and targets is a measure of model accuracy. The $R$ value for the entire dataset (training, validation and testing) is 0.99967, and it represents high correlation. In addition, all the categorized $R$-values (training, validation and test) are very close to 1 (see Fig. 7). When comparing both the measured and the predicted $F_z$ values the highest discrepancy observed is 2.18%. In the case of $M_z$, the best network architecture for the prediction of the experimental values was the 3-8-1 topology. The $R$ value for all the dataset (training, validation and testing) is 0.99978 and in each one of them separately is close to 1. As a result, the network achieves high accuracy (see Fig. 7). When comparing the measured with the predicted $M_z$ values the highest difference observed is 3.15%. From the output of both cases, it

![Comparison of the experimental values with the predicted values for a) $F_z$ and b) $M_z$](Fig. 8)
is concluded that the training of the ANN with one output for each case offers greater accuracy than in the case of the network with two outputs.

3 COMPARISON BETWEEN RSM AND ANN MODELS

A full factorial experimentation design is implemented to search for the effects of the cutting parameters (i.e. cutting speed, feed rate, and tool diameter) on the thrust force and torque in the case of drilling.

After each hole was made, the measurements of thrust force and torque were documented. Artificial neural network and response surface methodology models were developed to predict the thrust force and torque using the experimental data.

A comparison was established between the experimental values of $F_z$ and $M_z$ (see Fig. 8) and their values of ANN and RSM model, respectively. It is obvious that the predicted values from both models approximate the experimental values. Nevertheless, the predicted values from the ANN more accurately predict the experimental values than the regression analysis model. This can also be proved from the calculated percentage of error between experimental and predicted values of the models which are depicted in Fig. 9 for both the $F_z$ and the $M_z$. In the case of
the ANN models, the accuracy achieved was 2.18 % and 3.15 % for both the thrust force and torque, while in the case of the response surface methodology model the accuracy achieved was 3 % and 5.6 %, respectively.

4 CONCLUSIONS

The optimization of a drilling process focused on cutting tools and parameters is a basic part of the entirely machining process, which influences sustainability. The aim of this study was the generation of mathematical models for the prediction of the thrust force ($F_z$) and torque ($M_z$) related to the cutting tools and other crucial cutting parameters as feed rate and cutting velocity during the drilling process. Two modelling techniques the RSM and ANN were used to predict the thrust force and torque in a series of drilling operations of Al7075. The developed models were considered to be very accurate for the prediction of the $F_z$ and $M_z$ within the range of the manufacturing parameters used. A number of different ANN architectures (3-(6~12)-2) and (3-(6~12)-1) have been tested to obtain the best neural network configuration in each case. Finally, the best architecture was the (3-10-1) for the case of the thrust force and the (3-8-1) for the case of torque. The outcomes proved that the accuracy achieved was 2.18 % and 3.15 % when using the ANN models for both the thrust force and torque measured, respectively. In the case of the RSM model, the accuracy achieved was 3 % and 5.6 %, respectively. As a result, both strategies are suitable for modelling and predicting thrust force and torque when drilling is concerned, but the application of ANN is slightly more accurate than the RSM one.

5 ACKNOWLEDGEMENTS

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6 REFERENCES


Modelling and Prediction of Thrust Force and Torque in Drilling Operations of Al7075 Using ANN and RSM Methodologies


