A Transient Feature Learning-Based Intelligent Fault Diagnosis Method for Planetary Gearboxes

Bo Qin, Z. X. Li, Y. Qin

1 Inner Mongolia University of Science & Technology, School of Mechanical Engineering, China
2 Singapore University of Technology and Design, Engineering Product Development Pillar, Singapore

Sensitive and accurate fault features from the vibration signals of planetary gearboxes are essential for fault diagnosis, in which extreme learning machine (ELM) techniques have been widely adopted. To increase the sensitivity of extracted features fed in ELM, a novel feature extraction method is put forward, which takes advantage of the transient dynamics and the reconstructed high-dimensional data from the original vibration signal. First, based on fast kurtosis analysis, the range of transient dynamics of a vibration signal is located. Next, with the extracted kurtosis information, with variational mode decomposition, a series of intrinsic mode functions are decomposed; the ones that fall into the obtained ranges are selected as transient features, corresponding to maximum kurtosis value. Fed by the transient features, a hierarchical ELM model is well-trained for fault classification. Furthermore, a denoising auto-encoder is used to optimize input weight and threshold of implicit learning node of ELM, satisfying orthogonal condition to realize the layering of its hidden layers. Finally, a numerical case and an experiment are conducted to verify the performance of the proposed method. In comparison with its counterparts, the proposed method has a better classification accuracy in the aiding of transient features.

Keywords: transient features, kurtosis information, extreme learning machine, variational mode decomposition, fault diagnosis for planetary gearbox

Highlights

• VMD decomposition is employed to decompose signal into components.
• Kurtosis information is used to identify transient features in decomposed components.
• A high-dimensional feature vector is constructed using multiscale permutation entropy.
• A traditional extreme learning machine is optimized by introduction of a denoising auto-encoder.
• Comprehensive comparisons are given to show the efficacy of the proposed method, including both a numerical case and a practical planetary gearbox platform.

0 INTRODUCTION

With the advantages of compact structure, high transmission efficiency, and strong carrying capacity, the planetary gearbox has been widely adopted in transmission system powered devices, such as crawler vehicles, ships, and wind-driven generators [1]. Practically, the transmission system always works in adverse environments but suffers from continuously varying load. As a crucial component in a transmission system, the planetary gear is more prone to failure in poor working conditions. If faults in the planetary gear cannot be timely detected, it is possible that the whole transmission system may be disturbed and degenerated, leading to major safety threats. Therefore, providing prompt and reliable fault diagnosis ability for planetary gearboxes has received extensive attention and been an active research field.

With ever-increasing developments in sensor and data storage technologies in industrial fields [2] and [3], massive amounts of data have become available and affordable. For the planetary gearbox, vibration sensors have been widely installed, and the collected data contain important features to indicate their health state. Data-driven methods show their superiorities in fault diagnosis in comparison with mechanism model-based methods, in which a priori process knowledge is necessary but difficult to obtain. Commonly, it includes two sequential steps to develop data-driven fault diagnosis model: fault feature extraction and development of diagnosis model. Correspondingly, a series of related research studies are reviewed from these two aspects.

With respect to feature extraction, wavelet transformation [4] has been used in early stages; however, it faces the difficulty of selection proper basis functions. Also, once a basis function is determined, it cannot be adjusted in sequential analysis, leading to a non-optimal solution. After that, empirical mode decomposition (EMD) [5] and [6] was proposed; it decomposed the original measurements into several orthogonal components called intrinsic mode function (IMF). Each IMF corresponds to a specific frequency and is independent with each other. To overcome the problem of mode confusion, ensemble EMD (EEMD) [7] was proposed by adding Gaussian white noise into
Generally, the vibration signal of a planetary gearbox is complex and shows strong non-stationarity and modulation characteristics, resulting in the increase of difficulties for feature extraction. In fact, transient features in variation signal are sensitive to fault information. Correspondingly, if transient features in the vibration signal of the planetary gear box can be properly captured, it is possible to further improve fault diagnosis accuracy with advanced AI methods.

To achieve more accurate fault diagnosis performance, an intelligent fault diagnosis method is proposed for a planetary gearbox in this paper, which integrates advantages of fast spectral kurtosis, VMD, improved multiscale permutation entropy (MPE), and denoised AE (DAE) optimization. First, the vibration signal of planet gearbox is decomposed using fast kurtosis mapping and VMD decomposition. In this way, the centre frequency corresponding to several IMFs is captured to sensitive transient impact. Next, an extreme learning machine (ELM) method is used to construct an initial fault diagnosis model with extracted kurtosis features. After that, DAE is used to optimize the input weights and thresholds of the ELM hidden layer node to satisfy orthogonal conditions to realize the hierarchical hidden layer. In this way, the number of input and output samples is equal, improving the classification accuracy of the planetary gearbox fault diagnosis model with DAE-ELM. Experiments on real data show that the proposed method has higher diagnosis accuracy.

The rest of the paper is organized as follows. The preliminaries are briefly reviewed in Section 1. Section 2 introduces the proposed method. The experimental results and discussions are given in Section 3. Conclusions are drawn in Section 4.

1 PRELIMINARY

1.1 Fast Spectral Kurtosis

Kurtosis information is sensitive to transient shock, which can be used to present the transient frequency of a signal in a planetary gearbox. Antoni et al. [18] proposed a fast-spectral kurtosis algorithm based on FIR bandpass filter, in which one third of the range of a full-band was used with a binary tree structure. Signal $X(k)$ is decomposed into the pre-defined number of layers. After obtaining the filtering result of each layer, kurtosis values of all frequency segments are calculated below,

$$K(f) = \frac{\langle |c_i^f(k)|^4 \rangle}{\langle |c_i^f(k)|^2 \rangle^2} - 2, \quad (i = 0, 1, \ldots, 2^n - 1),$$  

(1)
where $f$ is the frequency of the signal; $c_m^i(t)$ is the filtering result obtained by the $i^{th}$ filter of the $m^{th}$ layer; $\langle \cdot \rangle$ denotes modulus value; $|$ stands for expected value.

The defined $K(f)$ is a measure of the peak value of the signal probability density function at a certain frequency. The interval between the centre frequency $f_c$ and the bandwidth $B_w$ corresponding to the maximum kurtosis value $K_{\text{max}}$ of $X(k)$ is calculated.

### 1.2 VMD Decomposition

To overcome modal aliasing and other drawbacks in both EMD and EEMD, VMD was proposed by Dragomiretskiy and Zosso [13]. It decomposes signal in a variational framework and uses iteration to find the optimal solution of the constrained variational model. A customized component $f$ is constructed to derive IMF, and the corresponding constraint variation model is given below,

$$
\begin{align*}
\min_{u_k, \omega_k} & \left\{ \sum_{k=1}^{n} \left\| \mathcal{L}_i \left[ \delta(t) + \frac{f}{\pi} \right] u_k(t) \right\|_2 \right\} \\
\text{s.t.} & \sum_k u_k = f,
\end{align*}
$$

where $f$ is the original signal, $u_k(t)$ is the $k^{th}$ IMF component, $\omega_k$ is the centre frequency of the $k^{th}$ component, $\delta(t)$ is the Dirac function, and $t$ is time index.

By solving Eq. (2) iteratively with the alternating direction multiplier method, it is transformed into an unconstrained problem. Through the above process, $K$ IMF components $u = [u_1, u_2, \ldots, u_K]$ and corresponding frequency centre $\omega = [\omega_1, \omega_2, \ldots, \omega_K]$ are obtained.

### 2 METHODOLOGY

In this section, an intelligent method is proposed to perform fault feature extraction and online diagnosis for a planetary gearbox. The basic structure and framework of the proposed method are given in Fig. 1, which includes three parts. First, in the data acquisition stage, through the sensor and acquisition device, the state monitoring system is used to collect the historical data and online data of planetary gearbox. Then, during the feature extraction stage, historical data are used to obtain fault feature components and their corresponding feature vectors through VMD, fast spectral kurtosis analysis, and an improved feature enhancement method based on a multiscale permutation entropy is used to filtrate feature vector sets. After that, based on DAE-optimized ELM algorithm, an intelligent state identification model is constructed by learning the historical data feature vector sets. Similarly, high quality eigenvector sets are obtained from online data through VMD and fast spectral kurtosis analysis and improved MPE methods. The high-quality feature vector set of online data is further used to train the state identification model of DAE-ELM based on historical data, so as to improve the fault classification accuracy of this mode and achieve the purpose of online diagnosis.

### 2.1 Construction of Feature Set

#### 2.1.1 Extraction of IMFs

Fig. 2 shows the details about the construction of the feature set. First, the vibration signal $X(k)$ is decomposed by VMD to obtain $n$ IMF components, and the centre frequency $f_i$ of each component is calculated. The vibration signal $X(k)$ is analysed to obtain the centre frequency $f_c$ and bandwidth $B_w$ corresponding to the maximum kurtosis value using FSK. Then, according to whether the centre frequency $f_i$ of the $i^{th}$ IMF component is within the frequency range $[f_c-B_w/2, f_c+B_w/2]$, a part of the IMFs is selected from the total IMFs as the fault
feature components, which is defined as a set \( Q \). The remaining IMF components will be discarded since they cover little fault information components. Finally, the IMF components in the set \( Q \) are added and reconstructed into a new time-domain waveform, and the IMPE value of each IMF component is calculated to construct the fault feature set \( T \), which will be specified in the following subsections.

Fig. 2. Signal decomposition and its feature vector construction

2.1.2 Improved Multiscale Permutation Entropy-based Feature Enhancement

Multiscale permutation entropy (MPE) algorithm [19] was designed to capture fine-grinded dynamics in various signals, including ECG signal, vibration and speech, etc. However, it still has the problem of learning the details of mutations. That is, first, the sample during coarse granulation is asymmetric. Second, for a specific time series \( X(i) \), as the scale \( s \) increases, the number of samples contained in the coarse-grained time series \( y_s(j) \) decreases exponentially, resulting in large fluctuations in the calculation of entropy value. To solve the above-mentioned problems, Azami and Escudero [20] used different scale factors \( s \) as independent variables to refine \( X(i) \) and calculate the average of the corresponding entropy values. The specific steps are as follows:

1. Coarse granulation under multiscale conditions. \( X(i) \) is coarsely granulated into \( y_s(j) \) and the result is given below,
   \[
   y_s(j) = \frac{1}{s} \sum_{i=(j-1)s+1}^{j} X(i),
   \]
   (3)

2. \( y_s(j) \) is further transformed into \( s \) different coarse-granulation sequences below,
   \[
   Z_i^{(s)} = \{y_{i,1}^{(s)}, y_{i,2}^{(s)}, \ldots, y_{i,s}^{(s)}\} \quad (i = 1, 2, \ldots, s),
   \]
   (4)

where \( y_{i,j}^{(s)} \) is as follow, \( y_{i,j}^{(s)} = \frac{1}{s} \sum_{i=0}^{s-1} x_{i+j}\) , where \( X(i) \) is time series with the length \( N \); \( s \) is time scale factor; and \( y_s(j) \) presents the coarse-grained sequence at different \( s, j=1, 2, \ldots, [N/s] \).

3. With independent variable \( s \), calculate the arranged entropy of each coarse-grained sequence \( y_s(j) \) and its average below,
   \[
   IMPE = \frac{1}{s} \sum_{j=1}^{s} PE(Z_i^{(s)}),
   \]
   (5)

where \( PE(\cdot) \) is the function to calculate permutation entropy.

2.2 Intelligent Diagnosis Model Construction

ELM has the advantages of fast operation speed and is a global optimal solution. However, the input weight and threshold of hidden layer nodes are randomly generated, resulting in the low accuracy and poor robustness of ELM. To solve this problem, DAE is employed to train ELM by adding local impairment noise to obtain a more robust network. The number of input and output samples is given the same value to achieve unsupervised learning. Also, weights \( A \) and \( B \) of the randomly generated hidden layer nodes satisfy the orthogonal condition, and the weight and threshold of the hidden layer of ELM are optimized to improve classification accuracy.

The orthogonal hidden layer parameters \( A \) and \( B \) are generated in DAE-ELM, the input sample set is mapped to the high dimensional space by Eq. (6) as follows,

\[
H = g(Ax + B) \quad \text{s.t. } A^T A = 1, \quad B^T B = 1,
\]
(6)

where \( a \) is the orthogonal weights that connect the input layer and the hidden layer node; \( A = [a_1, a_2, \ldots, a_N] \) and \( B = [b_1, b_2, \ldots, b_N] \) are an orthogonal threshold, in which \( a \) and \( b \) are nodes in the hidden layer; \( H \) is output matrix of the hidden layer.
The output weight $\beta$ is the learning conversion of the feature space to the input data calculated by Eq. (7) below,

$$\beta = \left( \frac{I}{C} + H^T H \right)^{-1} H^T x,$$

(7)

where $C$ is regularization coefficient.

The specific process of the algorithm is shown in Fig. 3.

Fig. 3. Flowchart of DAE optimized ELM

3 RESULTS

In this section, the performance of the proposed method is illustrated with two cases: a numerical case and an industrial one. Specifically, the first case verifies the decomposition result of signals, in comparison with that of EEMD. The second case focuses on analysing fault diagnosis performance with the proposed transient fault features.

3.1 Numerical Simulation

A simulation digital signal $X(k)$ is constructed from three independent components $X_1(k)$, $X_2(k)$, and $X_3(k)$, which are given in Eq. (8) as below,

$$X(k) = X_1(k) + X_2(k) + X_3(k)$$

$$= e^{-1000k} \sin(5000\pi k)$$

$$+ \cos(1000\pi k) \cdot \sin(150\pi k) + \cos(400\pi k),$$

(8)

where $X_1(k)$ is a periodic exponential decay shock signal with the frequency of 2500 Hz; $X_2(k)$ is a periodic frequency modulation signal; $X_3(k)$ is a cosine signal with the frequency of 200 Hz.

In Fig. 4, $X(k)$ and its components following Eq. (4) are plotted with the length of 1000 samplings. $X(k)$ is decomposed based on a five-layer fast kurtosis diagram, and the corresponding results are shown in Fig. 5. It is observed that the colour in the frequency range [2500 Hz, 5000 Hz] is the deepest, which can be used to infer the centre frequency and bandwidth. According to Eq. (1), the centre frequency $f_c$ is determined as 3750 Hz, and the bandwidth $B_w$ is 2500 Hz.

Fig. 4. The time domain waveform of $X(k)$ and its components

Fig. 5. Result of fast kurtosis diagram of simulated signal

Next, the decomposition results of $X(k)$ based on VMD are shown in Fig. 6, in which three IMFs are extracted, i.e. $IMF_{VMD1}$, $IMF_{VMD2}$, and $IMF_{VMD3}$. By comparing Fig. 6 with Fig. 4, it is observed that...
the extracted signals are similar to real components. $IMF_{VMD3}$ is similar to $X_1(k)$; $IMF_{VMD2}$ is similar to $X_2(k)$; and $IMF_{VMD1}$ is similar to $X_3(k)$. Therefore, the efficacy of VMD in signal decomposition is well illustrated, which provides a foundation for following the construction of a feature set. Further, EEMD is employed for comparison. Five IMFs are retained for EEMD, and the corresponding results are shown in Fig. 7. It is observed that the second component

![Image](image-url)

**Fig. 6.** VMD decomposition results of $X(k)$

![Image](image-url)

**Fig. 7.** EEMD decomposition results of $X(k)$

![Image](image-url)

**Fig. 8.** The constructed platform for fault diagnosis of planetary gearbox

![Image](image-url)

**Fig. 9.** Examples for typical fault and corresponding signal in typical fault states of planetary gearbox for a) broken tooth b) crack c) missing tooth, and d) wear of tooth surface
IMF_{EEMD_2} and the third component IMF_{EEMD_3} are mixed with each other. Besides, IMF_{EEMD_2} is mixed with the high-frequency component of IMF_{EEMD_1}, and the residual component cannot be decomposed. Therefore, it is concluded that the proposed method provides a more powerful feature extraction in comparison with competitive methods.

3.2 Experiments on Planetary Gearbox

In order to verify the effectiveness of the above algorithm, a practical testing condition shown in Fig. 8 is established. It contains a multi-channel data acquisition instrument branded SIEMENS-LMS and a DDS power transmission based comprehensive fault simulation platform produced by Spectra Quest.

For testing, four kinds of faults, (broken teeth fault, missing teeth fault, wear fault, and crack fault) occurring during the operation of the first-stage planetary wheel of the planetary gearbox are employed for analysis. During signal acquisition, the PCB356A16 accelerometer is used to collect the vibration signals of the vertical radial, horizontal radial and axial directions of the measuring point, the sampling frequency is 15,360 Hz, the motor speed is 2100 r/min, and 60 sets of data are collected in each status. Each group of data collection time is 1 second, that is, the number of sampling points corresponding to each group of data is 15,360. Intuitively, typical examples of these faults are given in Fig. 9, associated with a set of signals corresponding to each status.

3.2.1 Extraction of Sensitive Fault Features and Construction of Feature Set

Taking the broken tooth signal as an example, first, the fast kurtosis algorithm is used to obtain the centre frequency corresponding to the maximum kurtosis value of broken tooth signal and the results can be derived, as shown in Fig. 10.

![Fig. 10. Result of fast kurtosis diagram of broken tooth signal](image)

The centre frequency is identified as \( f_c = 2400 \) Hz, and the associate frequency band ranges from 2240 Hz to 2560 Hz. Then, the obtained signal is further decomposed by VMD, and the first six IMFs

<table>
<thead>
<tr>
<th>Status</th>
<th>No.</th>
<th>Eigenvector</th>
<th>Enhance multiscale entropy</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>PE1</td>
<td>PE2</td>
</tr>
<tr>
<td>Missing tooth failure</td>
<td>1</td>
<td>3.1822</td>
<td>4.3058</td>
</tr>
<tr>
<td></td>
<td>...</td>
<td>...</td>
<td>...</td>
</tr>
<tr>
<td></td>
<td>60</td>
<td>3.1703</td>
<td>4.2487</td>
</tr>
<tr>
<td>Normal</td>
<td></td>
<td>3.0615</td>
<td>4.0058</td>
</tr>
<tr>
<td></td>
<td>...</td>
<td>...</td>
<td>...</td>
</tr>
<tr>
<td></td>
<td>60</td>
<td>3.0403</td>
<td>3.9515</td>
</tr>
<tr>
<td>Broken tooth failure</td>
<td>1</td>
<td>3.5286</td>
<td>4.8606</td>
</tr>
<tr>
<td></td>
<td>...</td>
<td>...</td>
<td>...</td>
</tr>
<tr>
<td></td>
<td>60</td>
<td>3.5388</td>
<td>4.8242</td>
</tr>
<tr>
<td>Crack failure</td>
<td></td>
<td>3.9995</td>
<td>4.8846</td>
</tr>
<tr>
<td></td>
<td>...</td>
<td>...</td>
<td>...</td>
</tr>
<tr>
<td></td>
<td>60</td>
<td>3.9950</td>
<td>4.8680</td>
</tr>
<tr>
<td>Wear failure</td>
<td></td>
<td>4.3728</td>
<td>5.3764</td>
</tr>
<tr>
<td></td>
<td>...</td>
<td>...</td>
<td>...</td>
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<tr>
<td></td>
<td>60</td>
<td>4.2759</td>
<td>5.3332</td>
</tr>
</tbody>
</table>
are selected as candidate features, as shown in Fig. 11. Finally, $IMF_3$ is selected as the sensitive fault information since it locates in the frequency band that ranges from 2240 Hz to 2560 Hz.

Similarly, the same procedure is conducted on the other three fault signals and the normal signal. In the experiment, the sampling length is one second, and 60 sets of signals under each status are collected. Next, the improved MPE algorithm is used to calculate the entropy values of the above sixty groups of selected IMFs with twelve scales to construct feature vector set $T$. On the basis of this, Table 1 summarizes partial entropy values of all fault signals and normal signal since the limitation of page.

Table. 2. Accuracy comparison between the proposed method and its counterpart under each status

<table>
<thead>
<tr>
<th>Method</th>
<th>Missing tooth [%]</th>
<th>Normal [%]</th>
<th>Broken tooth [%]</th>
<th>Crack [%]</th>
<th>Wear [%]</th>
<th>Average [%]</th>
</tr>
</thead>
<tbody>
<tr>
<td>DAE-ELM</td>
<td>99</td>
<td>100</td>
<td>100</td>
<td>100</td>
<td>100</td>
<td>99</td>
</tr>
<tr>
<td>KELM</td>
<td>95</td>
<td>100</td>
<td>100</td>
<td>95</td>
<td>90</td>
<td>96</td>
</tr>
<tr>
<td>SVM</td>
<td>95</td>
<td>95</td>
<td>100</td>
<td>100</td>
<td>85</td>
<td>95</td>
</tr>
</tbody>
</table>

3.2.2 Diagnosis of Planetary Gearbox Faults

For each status in Table 1, 40 sets of eigenvectors are randomly selected as training samples, and the remaining twenty sets of data are used as testing data. The DAE-ELM intelligent diagnosis model for planetary gear is developed through the given steps in methodology.

In Fig. 12, the $X$-axis indicates the assignment of testing samples in each status. $Y$-axis indicates the type of fault, in which 1 is the missing tooth, 2 stands for normal status, 3 means a broken tooth, 4 is a crack, and 5 is wear. It is easy to see that there is only one missing sample in the crack fault. As a result, the classification accuracy of DAE-ELM intelligent diagnosis model reached 99 %.

For comparison, the feature vector set $T$ extracted in Subsection 3.2.1 is fed into KELM [21] and SVM [22] based diagnosis model, respectively. The results of these two methods are shown in Figs. 13 and 14, respectively. It is observed that two samples of wear fault in Fig. 13 is misclassified into the crack fault, and one sample of crack fault is misclassified in the wear fault. Also, one sample in missing tooth fault is misclassified in other faults. As a result, the accuracy of KELM based algorithm is 96 %. In Fig. 14, two
samples of wear fault are misclassified into crack fault, four samples of crack fault are misclassified, resulting in the average diagnosis accuracy is 95%. Therefore, the proposed DAE-ELM algorithm achieves the best performance by optimizing hidden layer of ELM using DAE.

This paper constructs a sensitive feature set and DAE-ELM intelligent diagnosis model for planetary gearboxes. Through the comparative analysis of simulated signal and experimental signal, the efficacy of the proposed feature set construction and the superiority of the DAE-ELM-based intelligent diagnosis model are verified. In comparison with the diagnosis method based on KELM and SVM, the results show that the proposed EMPE and DAE-ELM methods not only effectively extract sensitive transient characteristics of planetary gearbox vibration signals, but also the classification accuracy of the state identification model is increased by 3% and 4%, respectively.

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6 REFERENCES


