

# A method for calculating elliptic gear transmission efficiency based on transmission experiment

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Transmission efficiency is an important index to evaluate the transmission performance and energy consumption of gear transmission system. In order to analyze the transmission efficiency of elliptic gear, the load torque fluctuation model of elliptic gear is established to analyze the influence of load torque of elliptic gear transmission system on the torque of input and output. The torque data of input and output under different working conditions are obtained by building an elliptic gear transmission test. Finally, the transmission efficiency of the elliptic gear pair is obtained through the torque measurement data of the elliptic gear transmission test, and its variation law under different working conditions is analyzed. The results show that the transmission efficiency of the elliptic gear transmission system changes all the time, and presents an increasing trend with the increase of load torque and a decreasing trend with the increase of speed.

**Keywords:** elliptic gear, transmission test, load fluctuation, torque, transmission efficiency

## Highlights

- The torque fluctuation calculation model of elliptic gear is analyzed and established.
- The elliptic gear transmission test-rig is built, which can be used to obtain the corresponding dynamic data.
- The dynamic transmission efficiency of elliptic gear pair is calculated and obtained, and the influence of various operating parameters on the instantaneous transmission efficiency of the system is analyzed.

## 1 INTRODUCTION

With<sup>1</sup>the development of mechanical products towards complexity and diversification, the demand for high-performance non-uniform transmission mechanism is increasing day by day. The transmission mechanism represented by non-circular gear, which can achieve accurate and stable speed ratio, shows unique advantages in improving equipment performance and realizing special transmission requirements [1,2]. As a new type of gear transmission, elliptic gear is mainly used to transmit the non-uniform motion between two shafts, and realize the nonlinear relationship between the rotation angles of driving and driven parts [3,4]. The non-circular gear transmission system represented by elliptic gear has the characteristics of strong bearing capacity, compact structure and variable ratio transmission. It is mainly used in low speed and high torque occasions, such as rotary vane engine, hydraulic pump, hydraulic motor, printing press, packaging machine, textile equipment, spacecraft frequency converter, tank fire control system, continuously variable transmission (CVT), etc. [5,7]. In view of the expansion of its applications and the key role and special requirements in the transmission, it is meaningful to carry out in-depth research on the transmission efficiency of elliptic gear transmission system.

At present, a large number of research results have been accumulated for the transmission efficiency analysis method of gear transmission system. Diez [8] combined the tooth surface friction coefficient and transmission efficiency, analyzed the influence of the selection of

friction coefficient on the transmission efficiency of modified spur gear. Wang [9-14] carried out a detailed study on the transmission efficiency of gear transmission system. He combined tooth surface friction with power loss and tooth surface elasto-hydrodynamic lubrication, and proposed a calculation method of sliding friction loss of involute helical gear pair under load, considering assembly error, machining error, deformation and other factors. On this basis, the friction power loss and transmission efficiency of the gear transmission system under different working conditions and design parameters are analyzed, and the relevant data are obtained by building an experimental platform, which finally verifies the rationality of the proposed method. Petry [15] obtained the transmission efficiency of the system under the condition of high speed and variable torque by building a gear transmission test, and analyzed the change trend of the meshing efficiency of the gear transmission system and the total efficiency of the gearbox under the condition of different speed and load torque. Xu [16] proposed and established the calculation model of friction related mechanical efficiency loss of parallel shaft gear pair on the basis of comprehensively considering gear load distribution model, friction model and mechanical efficiency formula. Through gear transmission test, the effects of geometric parameters, tooth profile modification, working conditions, surface finish and lubricant performance on mechanical efficiency loss were analyzed. Based on the elasto-hydrodynamic lubrication model, Li [17] proposed a model to predict the load related power loss of spur gear pair. The instantaneous rolling and sliding shear in lubricating oil are determined by transient pressure distribution and oil film thickness distribution, so as to determine the mechanical power loss of gear meshing. Li [18] determined the calculation

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formula of the meshing efficiency of the conical involute gear based on the piecewise equivalent method, and analyzed the influence of different gear parameters on the contact line length, unit load and meshing efficiency in the meshing period. Liu [1-2] constructed a non-uniform end face movable tooth transmission mechanism by combining the end face movable tooth mechanism and non-circular gear pair, and analyzed the influence of tooth surface sliding friction on the transmission efficiency through simulation. Liu [19] analyzed the influence of time-varying meshing angle of non-circular gear pair on rolling rate loss caused by sliding friction and rolling friction by establishing a mathematical model of meshing efficiency of non-circular gear under elastohydrodynamic lubrication.

Although the above research results have irreplaceable guiding significance for the analysis of transmission efficiency of elliptic gear transmission system, most of the analysis of transmission efficiency of non-circular gear is only theoretical calculation, without systematic experimental analysis. In contrast, the experimental analysis can better reflect the authenticity and has more guiding significance. Therefore, this paper first analyzes the load fluctuation of the elliptic gear transmission system, and then extracts the torque data of the input and output ends by building the elliptic gear transmission test-bed and calculates and obtains the instantaneous transmission efficiency of the elliptic gear transmission system.

## 2 CALCULATION MODEL OF TRANSMISSION EFFICIENCY OF ELLIPTIC GEAR

Because of the variable ratio transmission characteristics of elliptic gear pair, its instantaneous transmission efficiency is always changing. The transmission efficiency of gear pair can reflect its load-carrying capacity and power loss, especially for elliptic gear which is suitable for low-speed and high torque condition. Therefore, it is of great significance to analyze its instantaneous transmission efficiency. In general, the transmission efficiency of elliptic gear system is defined as:

$$\eta = \frac{T_2}{T_1 i_{12}} \times 100\% \quad (1)$$

Where  $T_1$  represents the arithmetic mean value of input torque.  $T_2$  represents the arithmetic mean value of the output torque.  $i_{12}$  represents the transmission ratio of elliptic gear pair.

### 2.1 Pitch curve of elliptic gear

Fig.1 shows the pitch curve of elliptic gear. The center distance of elliptic gear pair is  $a$ , The rotation angles of driving and driven gears are respectively  $\theta_1$  and  $\theta_2$ . In the initial position,  $\theta_1 = \theta_2 = 0$ . The pitch curve equations of the driving and driven gears are as follows:

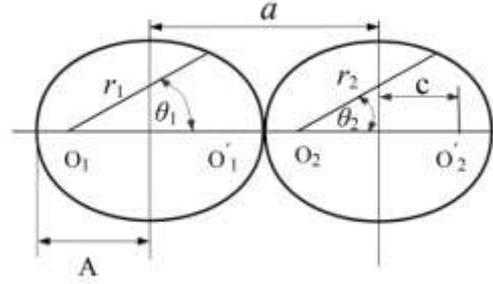


Fig. 1 Schematic diagram of elliptic gear pitch curve

$$r_1 = \frac{A(1-e_1^2)}{1-e_1 \cos(\theta_1)} \quad (2)$$

$$r_2 = \frac{A(1-e_2^2)}{1+e_2 \cos(\theta_2)} \quad (3)$$

Where,  $r_1$  and  $r_2$  represent the radius of pitch curve of driving gear and driven gear respectively.  $A$  is the long half shaft of elliptic gear.  $e_1$  and  $e_2$  are the eccentricity of the driving and driven gears respectively.  $c$  is the distance from the center of elliptic symmetry to the focus, and  $c = eA$ .  $\theta_1$  and  $\theta_2$  are the rotation angles of driving and driven gears respectively. There are the following relations between the rotation angles of driving and driven gears of elliptic gear pair:

$$\theta_2 = 2ac \tan \left[ \left( \frac{1+e_1}{1-e_1} \right) \tan \frac{\theta_1}{2} \right] \quad (4)$$

### 2.2 Torque of elliptic gear pair

The power transmission of elliptic gear pair is similar to that of cylindrical gear, and its transmission model is shown in Fig. 2 (a). Due to the time-varying curvature radius of the pitch curve of elliptic gears, there are certain differences among the teeth. Even if the load torque  $T_L$  on the driven shaft is constant, the torque fluctuation may occur on the driving side [20]. Therefore, in order to analyze the transmission torque of the elliptic gear pair, the load torque borne by the driven gear can be transformed into the driving gear, as shown in Fig. 2 (b).

The constant torque applied to the driven gear will lead to torque imbalance on the driving gear. Due to the time-varying transmission ratio function of elliptic gear pair, the driven gear will produce a certain moment of inertia in the case of variable angular velocity. Therefore, under the condition that the drive shaft rotates at a constant speed, the total torque required to drive the load torque can be expressed as:

$$T_1 = \frac{T_2}{i_{12}} = \frac{T_L + I_2 \alpha_2}{i_{12}} \quad (5)$$

Where  $T_1$  and  $T_2$  are the loads on the driving and driven gears respectively.  $T_L$  is the load torque.  $I_2$  is the moment of inertia of the driven gear.  $\alpha_2$  is the angular acceleration of the driven gear.

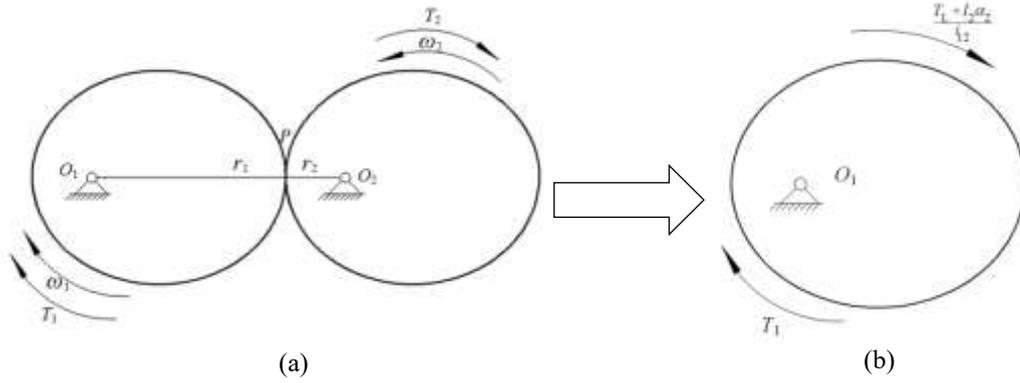


Fig. 2 Torque transmission model of elliptic gear pair

It can be seen from Fig. 2 that when the angle of the elliptic gear is  $\theta_1 = \omega_1 t$ . The design parameters of the two elliptical gears are the same, so  $e_1 = e_2$ . The transmission ratio of the elliptic gear pair can be expressed as:

$$i_{12} = \frac{a}{r_1} - 1 = \frac{1 + e_1^2 - 2e_1 \cos(\omega_1 t)}{1 - e_1^2} \quad (6)$$

Then, the angular velocity and angular acceleration of the driven gear can be expressed as:

$$\omega_2 = \frac{(1 - e_1^2) \omega_1}{1 + e_1^2 - 2e_1 \cos(\omega_1 t)} \quad (7)$$

$$\alpha_2 = \frac{d\omega_2}{dt} = -\frac{2\omega_1^2 e_1 (1 - e_1^2) \sin(\omega_1 t)}{[1 + e_1^2 - 2e_1 \cos(\omega_1 t)]^2} \quad (8)$$

Because the profile of elliptic gear is still involute, its moment of inertia can be calculated according to the method of cylindrical gear. The elliptic gear is approximately equivalent to a cam, and the moment of inertia per unit tooth width of the elliptic gear can be expressed as:

$$I = \frac{\rho_0 [a(1 - e_1^2)]^4}{2} \int_0^\pi \frac{d\theta_1}{(1 + e_1 \cos \theta_1)^4} \quad (9)$$

Let  $u = 1 + e \cos \theta_1$ , then equation (9) can be simplified as follows:

$$I = \frac{\rho_0 [a(1 - e_1^2)]^4}{2(e^2 - 1)^3} M \Big|_0^\pi = \frac{\pi \rho_0 [a(1 - e_1^2)]^4 (2 + 3e_1^2)}{4(1 - e_1^2)^3 \sqrt{1 - e_1^2}}$$

Where  $\rho_0$  is the density of elliptic gear and  $M$  is as follows.

$$M = \left[ \frac{(e_1^2 - 1)^2}{3} - \frac{5(1 + e_1 \cos \theta_1)(e_1^2 - 1)}{6} + \frac{2(1 + e_1 \cos \theta_1)^2 (e_1^2 - 1)}{3} + \frac{5(1 + e_1 \cos \theta_1)^2}{2} \right] \frac{e_1 \cos \theta_1}{(1 + e_1 \cos \theta_1)^3} + \frac{2 + 3e_1^2}{2\sqrt{1 - e_1^2}} \arcsin \left( \frac{e_1 + \cos \theta_1}{1 + e_1 \cos \theta_1} \right)$$

Substituting equation (6) to equation (9) into equation (5), we can get that:

$$T_1 = \frac{(1 - e_1^2) \left[ T_L (1 + e_1^2 - 2e_1 \cos(\omega_1 t))^2 - I_2 2e_1 \omega_1 (1 - e_1^2) \sin(\omega_1 t) \right]}{(1 + e_1^2 - 2e_1 \cos(\omega_1 t))^3} \quad (10)$$

### 3 CONSTRUCTION OF ELLIPTIC GEAR TRANSMISSION TEST

The elliptic gear test adopts horizontal mechanism, which is composed of precision mechanical system, measurement and control system, measurement software and other parts. The names and distribution positions of the main components of the test bench are shown in Fig. 3. The schematic diagram of its working principle is shown in Fig.4. The elliptical gear reducer is installed in the gear test platform, the input and output ends of the reducer are respectively connected through a coupling, and the signal is transmitted to the controller through computer control. The controller transmits the implementation command to the sensor and the driver, provides power and load by driving the motor, and then transmits the power and load to the reducer, so that the reducer can operate normally. The torque sensor and the vibration sensor sequentially collect the experimental data required to be measured and transmit them back to the computer through the controller to obtain the required experimental data. The built elliptic gear transmission test

is shown in Fig. 5.

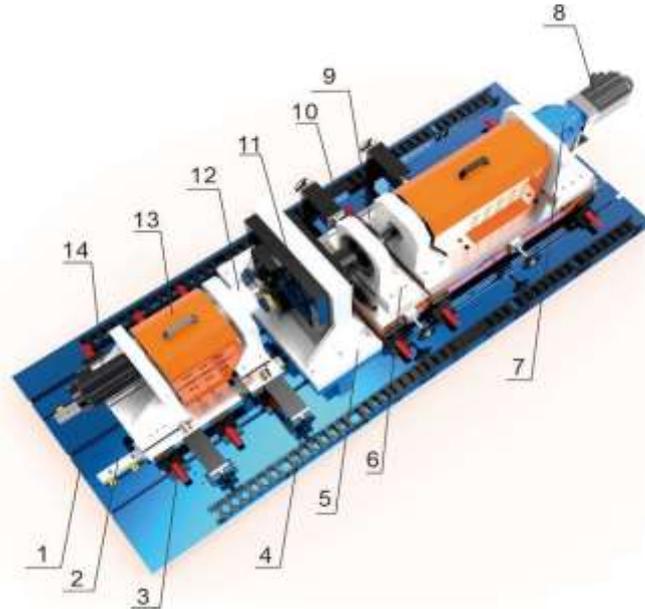


Fig. 3 The distribution of main engine components

1 T-groove cast iron platform base; 2 linear guide rail; 3 Locking device; 4 hand wheel; 5 reducer base; 6 base; 7 Test planetary reducer; 8 Servo motor at output end; 9 Circular grating protective cover at output end; 10 drag chain; 11 reducer under test; 12 input end circular grating protective cover; 13 protective cover; 14 input servo motor

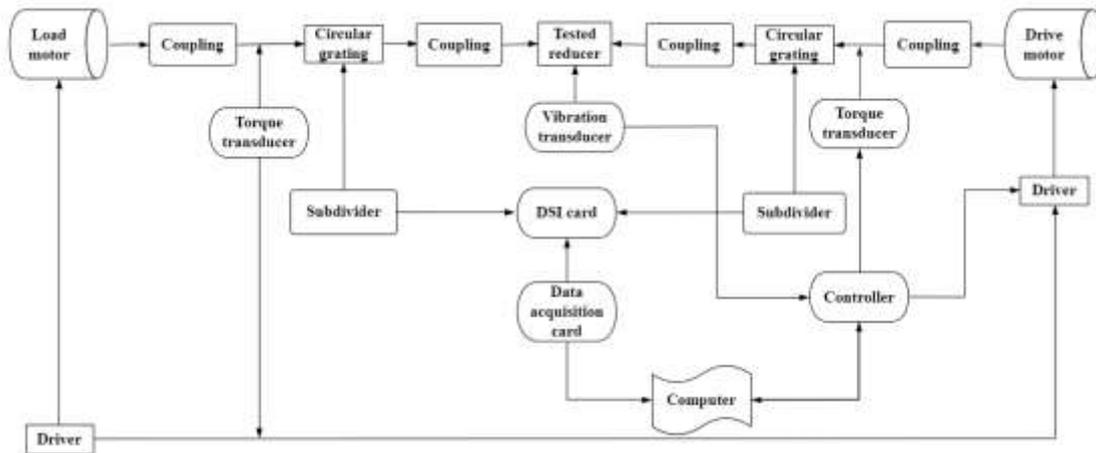


Fig. 4 Working principle of elliptic gear transmission test bench

The main machine of elliptic gear transmission test is mainly composed of mechanical system, including input end components, output end components, reducer mounting bracket and other parts. Each component is installed on the 2.6m long cast iron platform base with T-groove. The mounting bracket of the reducer is fixed in the middle of the base. The left side is the input end assembly and the right side is the output end assembly. The input end assembly includes input end motor slide plate (installing input servo motor and input torque sensor) and input end grating encoder slide plate (installing input grating encoder). The output end assembly includes output end grating encoder slide plate (installing output grating encoder) and output end loading support slide plate (installing output servo motor and output torque sensor). Each slide plate is installed on the linear guide rail, which can be moved left and right through the hand gear to adjust the position. The input end is driven by AC

servo motor, which can work in speed mode and torque mode respectively.

In order to realize the installation and test of different specifications and models of precision reducer, the test bench has designed precision mounting bracket and supporting multi specification precision mounting accessories (connecting disc, input shaft and output shaft), so as to improve the universality of the test equipment. The whole system is controlled by industrial computer, equipped with high-precision grating sensor system, high-precision torque sensor system and special measurement software, so as to realize the automatic measurement of the performance of precision reducer. The special feature of the test-bed is that it can be used for various types of reducers. The mounting bracket of the reducer is fixed in the middle of the base, and the linear guide rail is installed on the cast iron platform base. The movement of the input and output components is

realized through the gear rack mechanism.



(a)



(b)

Fig. 5 The elliptic gear transmission test

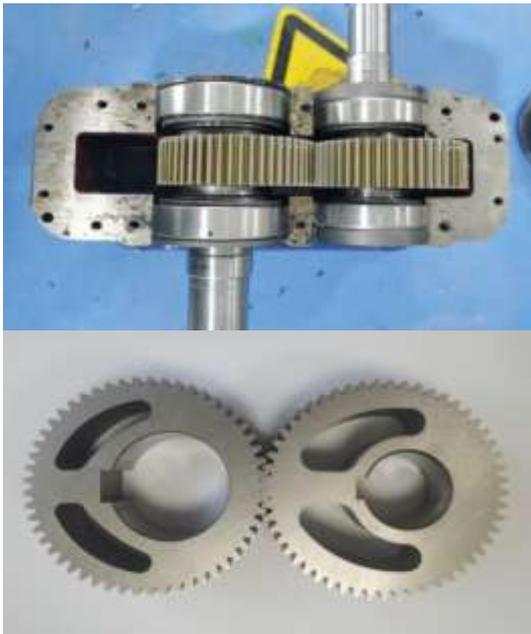


Fig. 6 The gear used in elliptic gear transmission experiment

The left hand gear in Fig.5(b) can ensure the implementation of lateral movement. There are similar mechanisms in the input end assembly and output end assembly, which can ensure the sliding of the input end motor and grating encoder slide plate, and realize the connection or disconnection between the encoder and the output shaft of the tested reducer and the connection or disconnection between the output torque sensor and the output shaft of the tested reducer. In Fig.5(b), the right hand gear can realize the vertical movement of the output component, which can make the slide plate of the input end grating encoder slide. So as to realize the connection

or disconnection between the input shaft of the measured reducer and the reducer, the slide plate of the input end motor, and the connection or disconnection between the grating encoder and the input end torque sensor. Fig. 6 shows the processed elliptic gear pair, and its design parameters are shown in Table 1.

Table 1 Elliptic cylinder gear design parameters

Parameter	Value
Module $m$ (mm)	1.5
Number of teeth $z$	53
Center distance $a$ (mm)	80
Tooth width $B$ (mm)	28
Eccentricity $e$	0.2
Pressure angle( $^{\circ}$ )	20
Equation of pitch curves	$r = \frac{38.4}{1 + 0.2\cos\theta}$
Material	Structural steel
Lubrication mode	Oil lubrication

#### 4 TORQUE FLUCTUATION OF ELLIPTIC GEAR

According to equation (10), the change trend of the torque of the driving and driven gears of the elliptic gear pair under different eccentricity and load torque conditions can be obtained, as shown in Fig. 7 to Fig. 8.

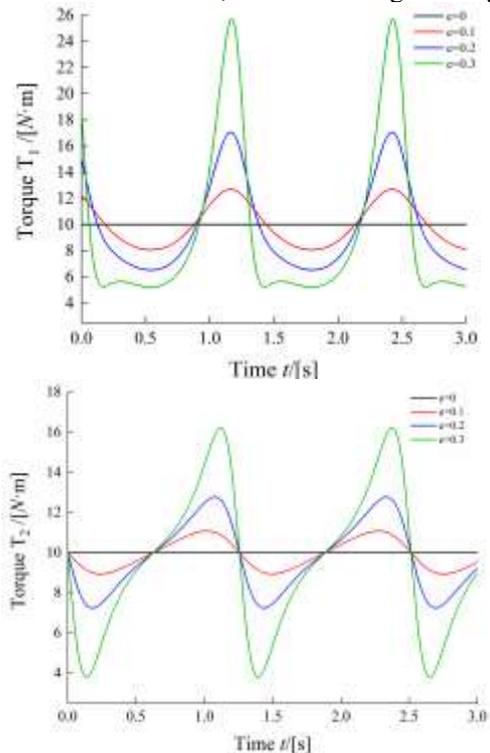


Fig. 7 Effect of eccentricity on torque of driving and driven gears

In Fig. 7, with the increase of eccentricity, the torque of the driving and driven gears of the elliptic gear increases. The change trend of driving gear is more

obvious. When the eccentricity is 0, the torque of the driving and driven gears of the elliptic gear pair is constant and will not fluctuate. When the eccentricity is not 0, the torque fluctuation of the driving and driven gears will occur. With the increase of eccentricity, the change of torque of driven gear is more regular. In contrast, the change of driving gear shows the same trend, but there are some differences between different eccentricities. This is because the driven gear is connected to the output and the torque at the output is constant. The driven gears move along a specific transmission ratio function under the driving gear. The inconsistency of the tooth profile of the elliptic gear pair makes the torque difference between the driving gears and the driven gears.

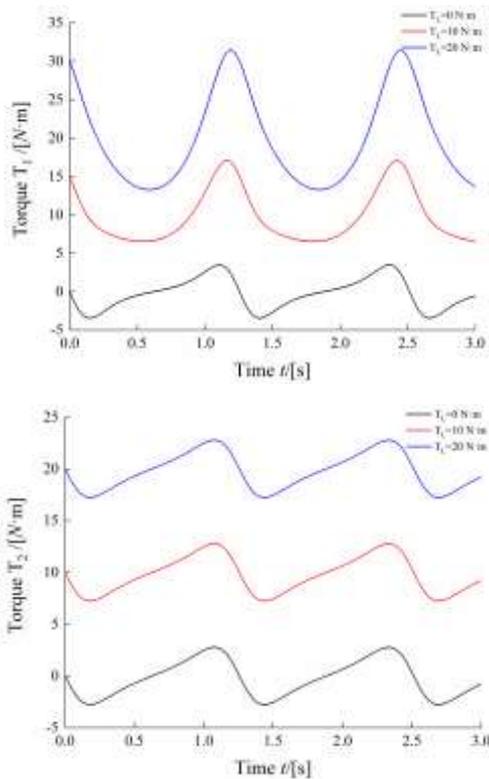


Fig. 8 Influence of load torque on driving and driven gear torque

In Fig. 8, with the increase of load torque, it also presents the same change trend. In contrast, the load change of driven gear is more uniform and smoother. The moment of inertia is produced by the non-uniform rotation of the elliptic gear. If the inertia moment is greater than the load moment, the torque of the driving shaft is opposite to the working driving direction, which will cause impact on the non-meshing tooth side of the gear. In Fig. 8, when the load torque is 0, that is, under no load condition, the minimum torque of the driving and driven gears of the elliptic gear pair will be less than 0, which is negative and shows a periodic trend. This shows that there are tooth surface separation and it will lead to the vibration and noise of the gear transmission system, which is not conducive to the normal work of the gear transmission system. With the increase of load torque, the

phenomenon that the minimum torque of driving gear and driven gear is less than 0 will disappear, which indicates that the existence of load will always lead to the phenomenon of tooth separation.

## 5 TRANSMISSION EFFICIENCY OF ELLIPTIC GEAR TRANSMISSION SYSTEM

In view of the inconsistency of elliptic gear tooth profile and the complexity of applicable working conditions, especially for reciprocating motion and forward and reverse motion (reversing device of pumping unit), it is necessary to analyze its transmission efficiency under the condition of forward and reverse motion so as to provide guidance for practical application. In the process of experiment, the rated output torque is preset. When the reducer is loaded from 0 to rated torque by driving motor, the torque data of input and output are collected. Each group collects 99 data points. The transmission efficiency of elliptic gear pair is analyzed by setting different operating parameters (torque and speed).

### 5.1 Torque analysis of elliptic gear pair

Fig. 9 to Fig. 11 shows the change trend of input shaft torque and output shaft torque under the condition of constant speed and increasing gradient of rated load torque.

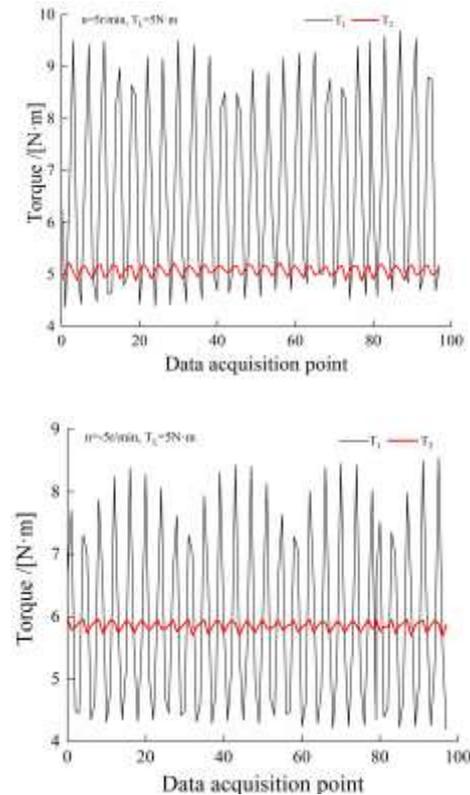


Fig. 9 The torque distribution law of elliptic gear pair when  $T_L=5N\cdot m$

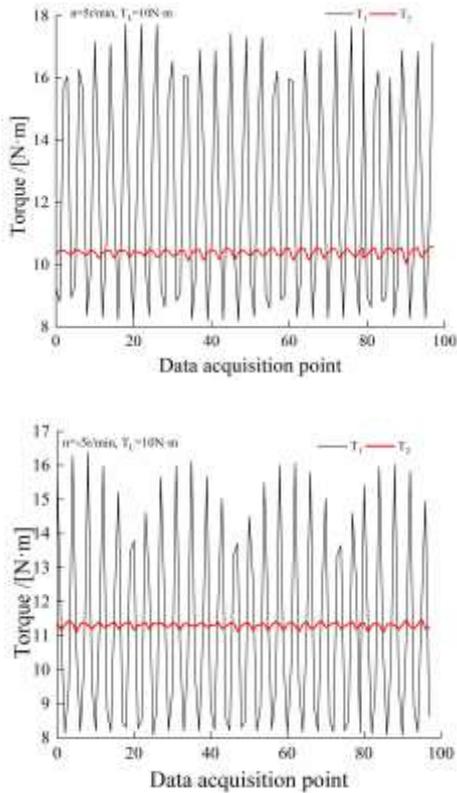


Fig.10 The torque distribution law of elliptic gear pair when  $T_L=10N\cdot m$

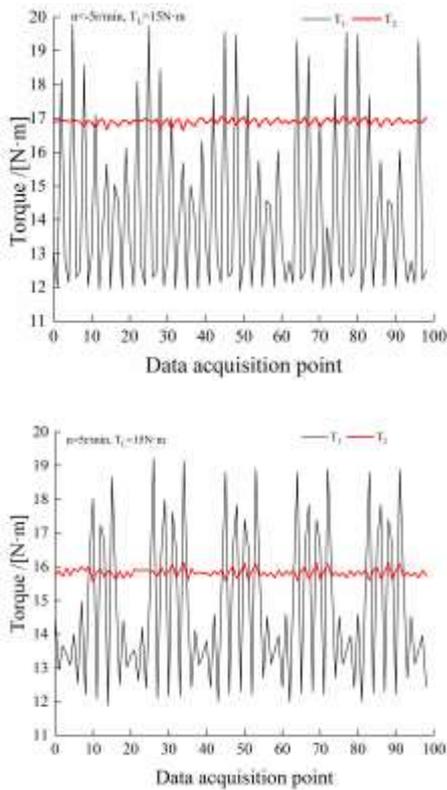


Fig. 11 The torque distribution law of elliptic gear pair when  $T_L=15N\cdot m$

With the increase of rated load torque, the torque of input

and output end is increasing. In contrast, the input and output torque in reverse case are larger than that in the case of positive rotation. The torque fluctuation of the output is small, and the input torque presents periodic change. With the increase of rated input torque, the difference between the two kinds of steering gradually increases. This is consistent with the torque fluctuation analysis results. The output torque is less than the input torque, that is, the torque  $T_1$  of the driving gear is greater than the torque  $T_2$  of the driven gear. Therefore, the correctness of the torque calculation method of the ellipse gear proposed in this paper is proved.

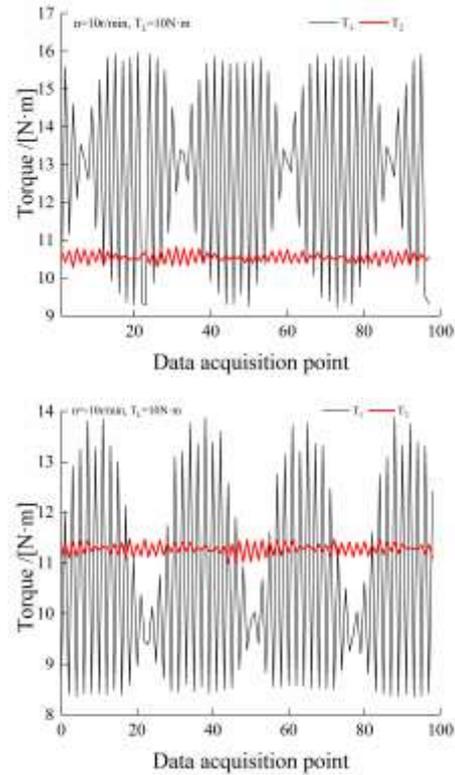


Fig. 12 The torque distribution law of elliptic gear pair when  $n=10r/min$

Fig. 12 to Fig. 13 show the change trend of input shaft torque and output shaft torque under clockwise and counterclockwise conditions when the load torque remains constant and the speed changes. According to the analysis in Fig. 9, with the increase of speed, the torque at the input and output end also presents a periodic trend. With the increase of the speed, the fluctuation of the torque at the input end and the torque at the output end is also intensified. Similar to the distribution trend in Fig. 8 ~ Fig. 10, the input and output torques under clockwise rotation are greater than those under counterclockwise rotation, which is related to the order of clockwise and counterclockwise rotation during the experiment. The first is the clockwise rotation experiment, and the second is the counterclockwise rotation experiment. Due to the existence of friction torque, starting torque and dynamic backlash between tooth profiles at the beginning of counterclockwise rotation after clockwise rotation, the torque under counterclockwise rotation is greater than

that under clockwise rotation. Consistent with the previous analysis results, the torque  $T_1$  of the driving gear is greater than that of the driven gear  $T_2$ , which further verifies the correctness of the torque calculation method of the elliptic gear proposed in this paper. It also shows that the change trend of the output torque and input torque of the elliptic gear transmission system will not change significantly with the increase of the speed, but there is a slight difference in the value.

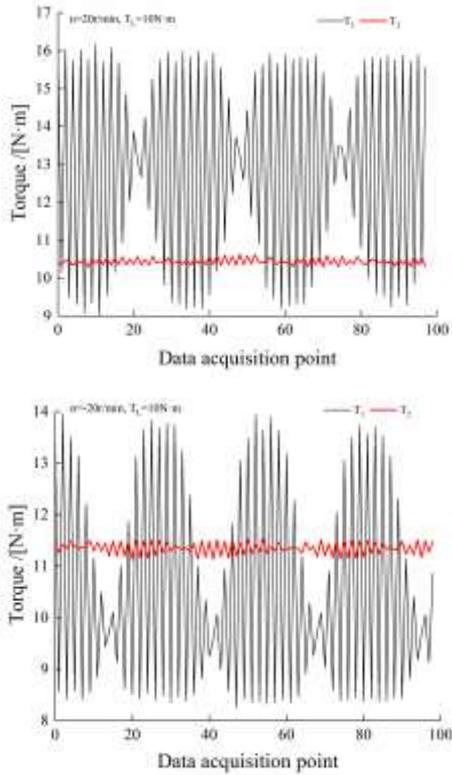


Fig. 13 The torque distribution law of elliptic gear pair when  $n=20r/min$

There is a certain error in the data collection process, this will cause a certain difference between the torque  $T_1$  at the input end and the torque  $T_2$  at the output end, which will affect the instantaneous transmission efficiency calculation of the gear transmission system. The way we reduce the error is to collect data multiple times, and the trend of the collected data is basically consistent with the theoretical analysis, which also verifies the correctness of our experiment.

## 5.2 Analysis of transmission efficiency of elliptic gear pair

Fig. 14 to Fig. 16 show the distribution law of instantaneous transmission efficiency calculated by equation (1) while keeping the speed constant and the rated load torque  $T_L$  gradient changing. Under the two steering conditions, the instantaneous transmission efficiency of elliptic gear pair changes all the time. In contrast, the transmission efficiency of counterclockwise transient is greater than that of clockwise transient. With

the increase of rated load torque, the instantaneous transmission efficiency of elliptic gear pair gradually presents a periodic trend, and the periodicity is more obvious.

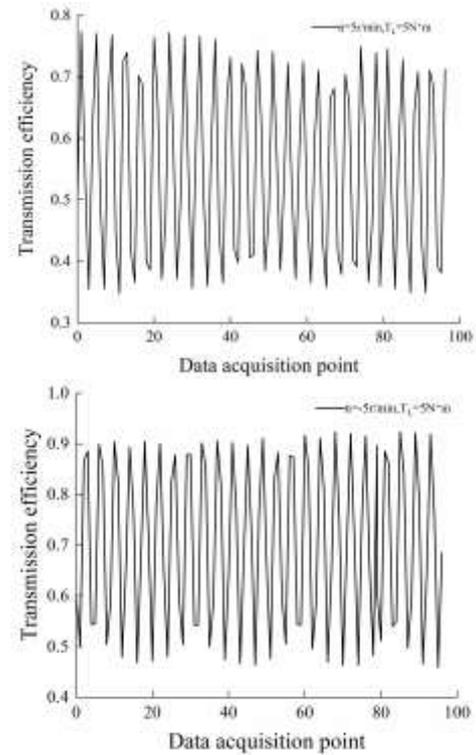


Fig. 14 The transmission efficiency of elliptic gear when  $T_L=5N·m$

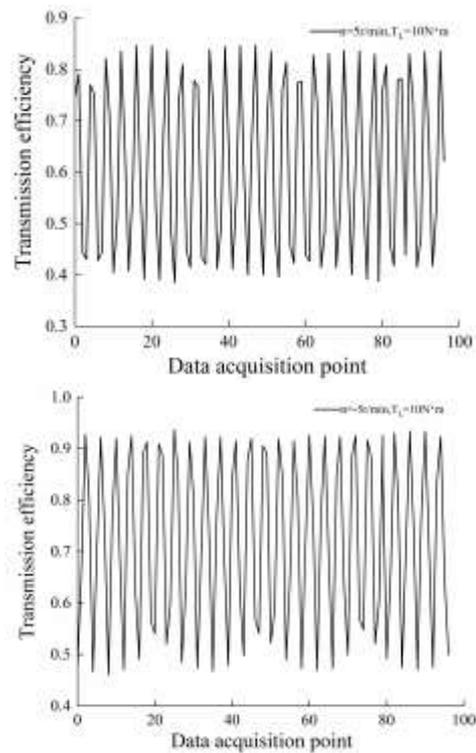


Fig. 15 The transmission efficiency of elliptic gear when  $T_L=10N·m$

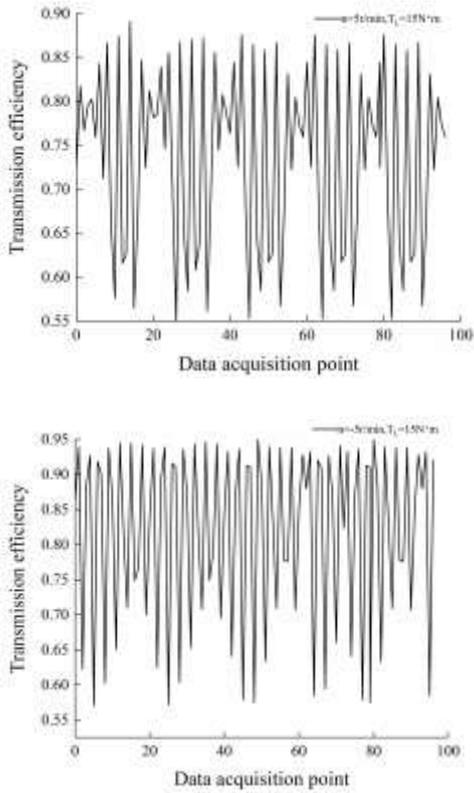


Fig. 16 The transmission efficiency of elliptic gear when  $T_L=15N\cdot m$

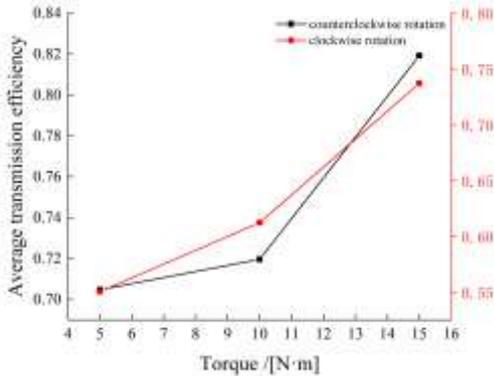


Fig. 17 The variation trend of transmission efficiency of elliptic gear with torque

Fig.17 shows the change trend of average transmission efficiency of elliptic gear pair with the change of load torque. With the increase of the load torque, the transmission efficiency of the elliptic gear pair shows an increasing trend. Therefore, on the premise of meeting the actual working conditions and the established motion law, increasing the load torque is conducive to improving the transmission efficiency of elliptic gear pair.

Fig. 18 to Fig. 20 show the distribution law of instantaneous transmission efficiency of elliptic gear pair under clockwise and counterclockwise conditions when the load torque remains constant and the speed gradient changes. It is consistent with the previous analysis when the speed is constant and the load gradient changes, and the transmission efficiency in counterclockwise transient

is greater than that in clockwise transient. However, under the two steering conditions, there is a periodic trend, and with the increase of speed, the periodicity is gradually obvious. In contrast, the counterclockwise transmission efficiency is greater than the forward transmission efficiency, and the transmission efficiency decreases with the increase of speed.

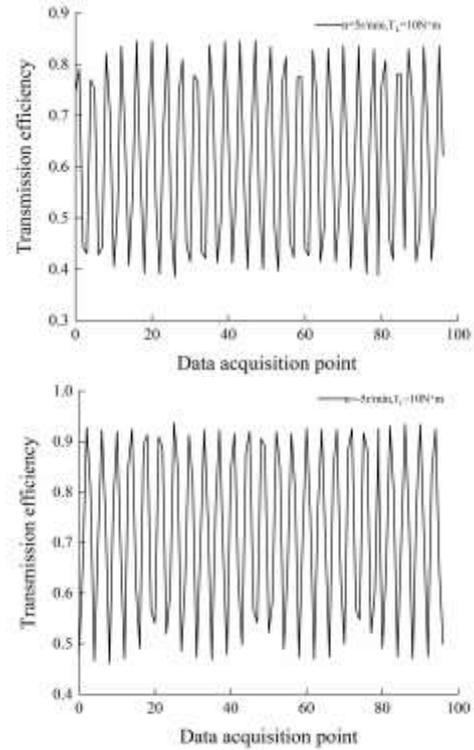


Fig. 18 Transmission efficiency of elliptic gear when  $n=5r/min$

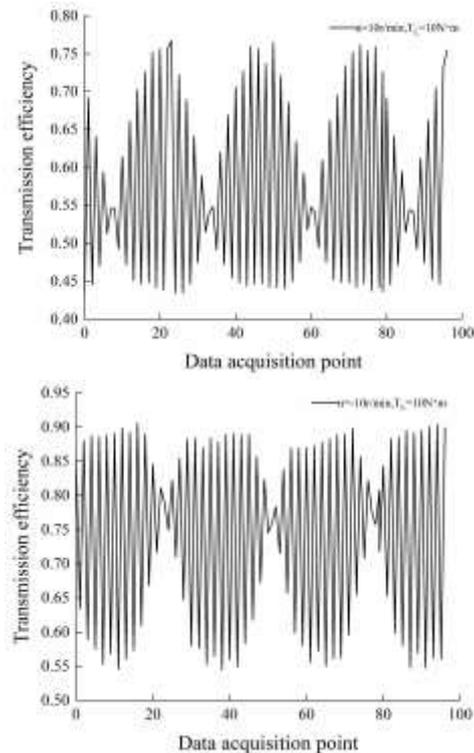


Fig. 19 Transmission efficiency of elliptic gear when  $n=10r/min$

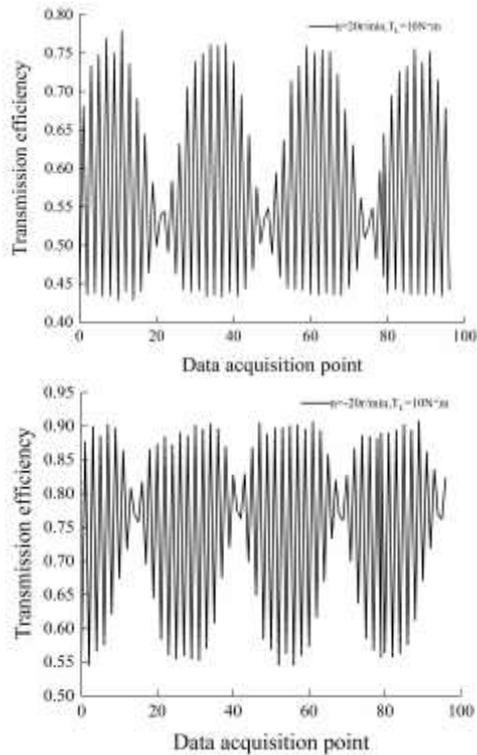


Fig. 20 Transmission efficiency of elliptic gear when  $n=20r/min$

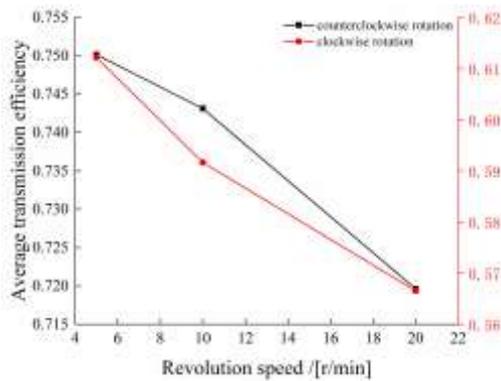


Fig. 21 The variation trend of elliptic gear transmission efficiency with torque

Fig.21 shows the change trend of the average transmission efficiency of clockwise and counterclockwise rotation of elliptic gear pair with the change of speed. With the increase of rotation speed, the average transmission efficiency clockwise and counterclockwise rotation of elliptic gear pair presents a decreasing trend. This is closely related to the non-linear change of instantaneous coincidence degree and transmission ratio of elliptic gear. Therefore, the elliptic gear pair can present high instantaneous transmission efficiency at low speed. In the process of engineering application, the instantaneous transmission efficiency can be improved by appropriately reducing the speed on the premise of meeting the established working conditions and motion rules.

Due to the inconsistency of the tooth profile of the elliptic gear, the instantaneous transmission efficiency during the meshing process changes all the time, and its

transmission efficiency will be lower than that of a general cylindrical gear. However, the elliptic pair is mainly suitable for low-speed, high-torque occasions, and is suitable for some special variable-speed sports occasions. Therefore, under the conditions of low speed and high torque, its instantaneous transmission efficiency can reach more than 80%, which can meet the requirements of working conditions.

## 6 CONCLUSIONS

Based on the load fluctuation model of elliptic gear, the test-bed of elliptic gear transmission is built, and the torque data values of input and output in forward and reverse rotation are obtained. On this basis, the transmission efficiency of elliptic gear pair is calculated and obtained, and the influence of load torque and speed on the transmission efficiency of the system is analyzed. The results show that:

1) Due to the time-varying pitch curve radius of elliptic gear pair, the tooth profile is inconsistent, which makes the torque at the input end and output end have certain differences under the conditions of forward rotation and reverse rotation, so the transmission efficiency will have certain differences. Under the action of load torque, the torque on the driving and driven gears of elliptic gear will increase with the increase of eccentricity and load torque of elliptic gear.

2) The load torque and speed have a certain influence on the transmission efficiency of elliptic gear transmission system. The transmission efficiency will decrease with the increase of speed and increase with the increase of load torque, which also shows that the non-circular gear transmission system represented by elliptic gear is really suitable for low speed and high torque conditions.

3) In view of the commonness of elliptic gear and non-circular gear and the subordinate relationship between them, the calculation method and experimental means of transmission efficiency of elliptic gear proposed in this paper can be used for other types of non-circular gear transmission system, and can provide some theoretical guidance for the calculation of transmission efficiency.

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