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Analysis of EDM Process Parameters on Inconel 718 Using the Grey-Taguchi and Topsis Methods

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Nickel-based superalloys are gaining importance for their growing usage in aerospace industries. Amidst the various advanced machining processes, electro discharge machining (EDM) is considered to be an important one for its ability to machine materials irrespective of its intrinsic properties. In this study, Inconel 718 is considered as a work material, and an L_{18} orthogonal array (OA) experimental plan is utilized to machine the work material. The influential factors, which affect the EDM performance characteristics, are identified using analysis of variance (ANOVA). Not much work has been done regarding using grey-Taguchi technique for order of preference by similarity to ideal solution (TOPSIS) methods, although these methods can be easily applied for multi-objective optimization. These methods provide the best results with the available sparse data. The best combination of machining factors is determined using grey-Taguchi and TOPSIS methods. Based on the conducted experiments, voltage (V) and pulse off-time (t_{off}) show a notable contribution on output performance. The optimal combination of input parameter through grey-Taguchi is found to be 10 A, 30 V, 200 µs, and 20 µs respectively, for the EDM parameters: current (I), V, pulse on-time (t_{on}) and t_{off} for improved response. Moreover, the best parameter setting (I = 10 A, V = 30 V, t_{on} =100 µs and t_{off} = 20 µs) is identified using the TOPSIS method for the performance measures machining rate (MR), tool wear rate (TWR), overcut (OC), and taper overcut (TOC). Further tool wear behaviour is also studied through scanning electron microscope (SEM) images by varying the voltage.

Keywords: Inconel, ANOVA, grey-Taguchi, overcut, taper

Highlights

- EDM process parameters(voltage, current, pulse on- time and pulse off- time) were optimized through the L18 orthogonal
 experimental design method, and the grey relational analysis (GRA) method, considering multi-responses, such as machining
 rate (MR), tool wear rate (TWR), overcut (OC), and taper overcut (TOC).
- The methods grey-Taguchi and TOPSIS were used to study the influential parameters that provide the best results with the available sparse data.
- Based on GRA and TOPSIS, the optimum level parameters for EDM have been identified. Furthermore, the tool wear behaviour
 is also studied through SEM images by varying the voltage.
- The optimal combination of the input parameter to acquire better responses based on grey-Taguchi has been found to be (10 A), V (30 V), t_{on} (200 μs), and t_{off} (20 μs). According to ANOVA, the voltage and t_{off} plays a prominent role in machining Inconel 718.
- The best combinations identified using the TOPSIS method for better performance measures is 10 A, 30 V, 100 µs and 20 µs.

0 INTRODUCTION

Electro discharge machining (EDM) has a one-off significant process for the machining of hard materials and superalloys. Heat-resistant superalloys (HRSA), especially the Inconel alloy, find applications in aerospace and marine components, cryogenic storage tanks, and nuclear reactor components. Understanding the importance of the Inconel alloy, manufacturing scientists and engineers are attempting to understand the behaviour of it through EDM processes. In the machining of Inconel 718, Shen et al. [1] applied high-speed EDM with air as a dielectric medium and produced components with better surface quality. The importance of powder-mixed dielectric fluid in the EDM for machining Inconel alloy was analysed by Talla et al. [2]. The researchers revealed better results for surface quality and accuracy while using

different powders, such as graphite, silicon, and aluminium [3] and [4]. Torres et al. [5] investigated the behaviour of an Inconel 600 alloy through EDM process. They studied the electrical parameters' influence and concluded that the change in polarity has a significant influence on surface quality. Tanjilul et al.[6] reported that a novel flushing method and a machining current significantly influences the debris removal. The size of the debris particles increases with increasing machining current. Rajesha et al. [7] studied the effect of process parameters such as current, duty cycle, sensitivity control, inter-electrode gap control, and flushing pressure on the material removal rate (MRR) and surface roughness (SR). They found that the pulse current and duty factor has the highest influence. Kuppan et al. [8] reported that the MRR and SR increase with the increase in peak current, duty factor, and electrode speed.

Mohanty et al. [9] conducted an L₉ orthogonal array (OA) and optimized the EDM process parameters of Inconel 825 using grey relational analysis (GRA). The parameters combination ($I(1A), t_{on}(10 \ \mu s)$, and duty cycle (75 %)) showed good results for the rate of material removed, surface quality, and radial overcut. Mohanty et al. [10] highlighted the importance of cryogenic treatment of tool in EDM on output performance using technique for order of preference by the similarity to ideal solution (TOPSIS) method and teaching-learning-based optimization algorithm. Dang [11] optimized the EDM parameters using a kriging model and particle swarm optimization method, finding that the model and method is suitable for the optimization of EDM process. Lin et al. [12] optimized and enhanced the EDM process parameters for Inconel 718 through multi-objective optimization technique using grey-Taguchi. Muthuramalingam and Mohan [13] machined SS 201 through EDM and established the importance of peak current. Lin et al. [14] conducted experiments on Ti-6Al-4V alloy through Micro-EDM and studied the influence of process parameters and gaps using the grey relational analysis (GRA)-Taguchi technique. The use of the GRA with Taguchi technique yields better results for tool electrode wear and overcut.Based on the above literature, the characteristics of EDM for machining holes on Inconel 718 are influenced by various input parameters. Each performance characteristic has different combinations of optimal process parameters and thus, in the case of multiple responses, the selections of optimal machining parameters are difficult. The grey system, proposed by Deng [15], handles the vague information and thus the GRA method is recommended as a principal method for multiple response optimisation. Therefore, researchers optimized the machining of Inconel 718 using electrical parameters and inter-electrode gap (IEG). In this paper, EDM process parameters: I, V, t_{on} and t_{off} were optimized through the L₁₈ orthogonal experimental design method, and the GRA method considering multi-responses, such as machining rate (MR), tool wear rate (TWR), overcut (OC) and taper overcut (TOC). Not much work has been done using the grey-Taguchi and TOPSIS methods although these can be easily applied for multi-objective optimization. The significant contribution of this research is in using these methods to study the influential parameters that provide the best results with the available sparse data.Based on GRA and TOPSIS, the optimum level parameters for EDM have been identified. Furthermore, the tool wear behaviour is also studied

through scanning electron microscope (SEM) images by varying the voltage.

1 EXPERIMENTAL

The experimental set-up for EDM machining process is shown in Fig. 1. It consists of a maximum working voltage of 415 V. maximum current of 25 A. work table size of 600 mm \times 400 mm, a maximum electrode length of 400 mm, and a servomotor for inter-electrode gap control. Inconel 718 has been selected as a workpiece material, whereas a brass electrode of Ø 0.5 mm is used with EDM oil as the dielectric medium. Tables 1 and 2 provides the details of chemical and mechanical properties of Inconel 718 [16]. The thickness of workpiece is 3.1 mm. Since the discharge energy is primarily determined by current (I), voltage (V), pulse on-time (t_{on}) , and pulse off-time (t_{off}) , these factors are used as the input parameters. These parameters are selected based on the literature review, and levels are identified based the preliminary experiments; 10 A, 12 A and 14 A have been considered as current variables; 30 V, 40 V and 50 V have been chosen as voltage variables;100 µs, 150 μ s and 200 μ s have been chosen as t_{on} values with t_{off} values of 20 µs, 30 µs and 40 µs. Table 3 shows the experimental layout using an L₁₈ OA. MR is calculated by dividing the length of the through hole with the machining time required to complete the through hole. TWR is calculated using the relation mass is $\rho \times v$, where ρ is brass density, v volume of brass tool $(\pi r^2 h)$, h brass tool height. During the start and end of each



Fig. 1. Experimental setup

Table 1. Chemical composition of Inconel 718 (weight %)

| С | Mn | Si | Cr | Ni | Со | Мо | Nb+Ta | Ti | AI | Fe |
|-------|------|------|-------|-------|------|------|-------|------|------|-------|
| 0.040 | 0.08 | 0.08 | 18.37 | 53.37 | 0.23 | 3.04 | 5.34 | 0.98 | 0.50 | 17.80 |

experiment, the length of the brass tool is measured, and the difference is noted as *h*; this value is used to calculate the volume of brass electrode. The ratio of volume of electrode wear to the time taken to complete the experiment is called *TWR*. *OC* is calculated using optical microscopic images. *OC* is defined by $\Delta R = Re - Rt$, where *Re* is the entrance radius of the machined hole and *Rt* the tool electrode radius. The difference in *Re* and *Rt* results in *OC*. *TOC* is defined by TOC = D - d/(2L), where, *D* is entry diameter of the machined hole, *d* exit diameter of the machined hole, and *L* thickness of the workpiece.

Table 2. Mechanical properties of Inconel 718

| | | Tensile suess [IVIF a] |
|-----|------|------------------------|
| 388 | 1375 | 1170 |

2 RESULTS

MR is the measure of machinability of the material. Hence, for a characteristic like *MR*, "larger-the-better"

| | Table 3 | 3. L | 18 orthogona | l array |
|--|---------|------|--------------|---------|
|--|---------|------|--------------|---------|

is considered and the obtained *MR* data values are homogenized as shown below **[14]**:

$$x_{j}^{*}(i) = \frac{x_{j}(i) - \min x_{j}(i)}{\min x_{j}(i) - \min x_{j}(i)},$$
(1)

where $x_j^*(i)$ are the homogenized *MR* after the preprocessing, is the signal-to-noise ratio of the *MR*, where i=1 for *MR*; i=1,2,3,...,18 for experiments 1 to 18.

EDM performance is also measured using *TWR*, *OC* and *TOC*. Hence, to achieve better machining quality, the "smaller-the-better" is considered in view of minimizing *TWR*, *OC*, and *TOC*. Therefore the actual sequence must be normalized as follows [14]:

$$x_{j}^{*}(i) = \frac{\max x_{j}(i) - x_{i}(i)}{\max x_{j}(i) - \min x_{j}(i)},$$
(2)

where $x_0^*(i)$, $\Delta_{0j}(i)$, $x_j^*(i)$ are reference sequence, deviation sequence and comparability sequence, respectively.

$$\Delta_{0j}(i) = |x_0^*(i) - x_j^*(i)|.$$
(3)

| | | Range | of factors | | | A stud uslus a | 6 | |
|--------------|---|-------|----------------------|-----------------------|-------------|----------------|----------------|----------|
| Experiment - | А | В | С | D | - | Actual value o | r parameters | |
| NU. — | Ι | V | t _{on} [μs] | t _{off} [μs] | MR [mm/min] | TWR [g/min] | <i>OC</i> [mm] | TOC [mm] |
| 1 | 1 | 1 | 1 | 1 | 0.019137 | 0.00261 | 0.2419 | 0.04839 |
| 2 | 1 | 2 | 2 | 2 | 0.042738 | 0.00466 | 0.1630 | 0.06966 |
| 3 | 1 | 3 | 3 | 3 | 0.065654 | 0.00205 | 0.1978 | 0.03706 |
| 4 | 2 | 1 | 1 | 2 | 0.056586 | 0.00351 | 0.1885 | 0.05388 |
| 5 | 2 | 2 | 2 | 3 | 0.049971 | 0.00410 | 0.1328 | 0.03871 |
| 6 | 2 | 3 | 3 | 1 | 0.062078 | 0.00317 | 0.1398 | 0.04179 |
| 7 | 3 | 1 | 2 | 1 | 0.090978 | 0.00905 | 0.1398 | 0.01508 |
| 8 | 3 | 2 | 3 | 2 | 0.051362 | 0.00366 | 0.1143 | 0.06070 |
| 9 | 3 | 3 | 1 | 3 | 0.072961 | 0.00675 | 0.0911 | 0.04752 |
| 10 | 1 | 1 | 3 | 3 | 0.044799 | 0.00371 | 0.1398 | 0.03871 |
| 11 | 1 | 2 | 1 | 1 | 0.039450 | 0.00436 | 0.1027 | 0.04284 |
| 12 | 1 | 3 | 2 | 2 | 0.032244 | 0.00559 | 0.1444 | 0.04806 |
| 13 | 2 | 1 | 2 | 3 | 0.081764 | 0.00526 | 0.1537 | 0.03786 |
| 14 | 2 | 2 | 3 | 1 | 0.050321 | 0.00456 | 0.1491 | 0.05987 |
| 15 | 2 | 3 | 1 | 2 | 0.043268 | 0.00399 | 0.1003 | 0.04493 |
| 16 | 3 | 1 | 3 | 2 | 0.070008 | 0.00488 | 0.1676 | 0.06497 |
| 17 | 3 | 2 | 1 | 3 | 0.062579 | 0.00699 | 0.1235 | 0.11196 |
| 18 | 3 | 3 | 2 | 1 | 0.081983 | 0.00456 | 0.1769 | 0.09516 |

Similarly, other computation was carried out for 18 experiments and the values of all Δ_{0j} for j=1,2,3,...,18 are represented in Table 4.

In continuation of data preprocessing, a coefficient for grey relational analysis is found using the relation given below [14]:

$$\xi_{j}(i) = \frac{\Delta_{\min} + \zeta \cdot \Delta_{\max}}{\Delta_{0j}(k) + \zeta \cdot \Delta_{\max}}, \qquad (4)$$

where ζ is a unique coefficient and ζ is considered as 0.5 because all parameters are given equal weight.

The grey relational grade (GRG) presented in Table 5 is calculated by averaging the GRC and overall

| Table 4. | Performance | characteristics | of the proc | essed data |
|----------|-------------|-----------------|-------------|------------|
|----------|-------------|-----------------|-------------|------------|

| Experiment | Performa | ance characteris | tics after data pro | ocessing | | Deviation s | sequences | |
|---------------|----------|------------------|---------------------|----------|----------|-------------|-----------|--------|
| run reference | MR | TWR | OC | TOC | MR | TWR | OC | TOC |
| sequence | [mm/min] | [g/min] | [mm] | [mm] | [mm/min] | [g/min] | [mm] | [mm] |
| 1 | 0.0000 | 0.9197 | 0.0000 | 0.6562 | 1.0000 | 0.0803 | 0.0000 | 0.3438 |
| 2 | 0.3285 | 0.6270 | 0.5231 | 0.4366 | 0.6715 | 0.3730 | 0.5231 | 0.5634 |
| 3 | 0.6475 | 1.0000 | 0.2924 | 0.7731 | 0.3525 | 0.0000 | 0.2924 | 0.2269 |
| 4 | 0.5213 | 0.7921 | 0.3539 | 0.5995 | 0.4787 | 0.2079 | 0.3539 | 0.4005 |
| 5 | 0.4292 | 0.7069 | 0.7231 | 0.7561 | 0.5708 | 0.2931 | 0.7231 | 0.2439 |
| 6 | 0.5977 | 0.8399 | 0.6769 | 0.7243 | 0.4023 | 0.1601 | 0.6769 | 0.2757 |
| 7 | 1.0000 | 0.0000 | 0.6769 | 1.0000 | 0.0000 | 1.0000 | 0.6769 | 0.0000 |
| 8 | 0.4486 | 0.7697 | 0.8462 | 0.5291 | 0.5514 | 0.2303 | 0.8462 | 0.4709 |
| 9 | 0.7492 | 0.3289 | 1.0000 | 0.6652 | 0.2508 | 0.6711 | 1.0000 | 0.3348 |
| 10 | 0.3572 | 0.7634 | 0.6769 | 0.7561 | 0.6428 | 0.2366 | 0.6769 | 0.2439 |
| 11 | 0.2827 | 0.6695 | 0.9231 | 0.7135 | 0.7173 | 0.3305 | 0.9231 | 0.2865 |
| 12 | 0.1824 | 0.4937 | 0.6462 | 0.6596 | 0.8176 | 0.5063 | 0.6462 | 0.3404 |
| 13 | 0.8718 | 0.5416 | 0.5846 | 0.7649 | 0.1282 | 0.4584 | 0.5846 | 0.2351 |
| 14 | 0.4341 | 0.6418 | 0.6154 | 0.5377 | 0.5659 | 0.3582 | 0.6154 | 0.4623 |
| 15 | 0.3359 | 0.7221 | 0.9385 | 0.6919 | 0.6641 | 0.2779 | 0.9385 | 0.3081 |
| 16 | 0.7081 | 0.5952 | 0.4923 | 0.4851 | 0.2919 | 0.4048 | 0.4923 | 0.5149 |
| 17 | 0.6047 | 0.2939 | 0.7846 | 0.0000 | 0.3953 | 0.7061 | 0.7846 | 1.0000 |
| 18 | 0.8748 | 0.6418 | 0.4308 | 0.1734 | 0.1252 | 0.3582 | 0.4308 | 0.8266 |

Table 5. Computed Grey relational grade

| Europriment No | | GR | C | | Grey relational grade (GRG) |
|----------------|------------------|------------------|-----------------|-----------------|---|
| Experiment No. | $MR \xi_{i(1)}$ | TWR $\xi_{i(2)}$ | $OC \xi_{i(3)}$ | $MR \xi_{i(4)}$ | $y_i = 1/4 \cdot (\xi_{i(1)} + \xi_{i(2)} + \xi_{i(3)} + \xi_{i(4)})$ |
| 1 | 0.3333 | 0.8617 | 1.0000 | 0.5926 | 0.6969 |
| 2 | 0.4268 | 0.5727 | 0.4887 | 0.4702 | 0.4896 |
| 3 | 0.5865 | 1.0000 | 0.6310 | 0.6879 | 0.7263 |
| 4 | 0.5109 | 0.7063 | 0.5856 | 0.5552 | 0.5895 |
| 5 | 0.4669 | 0.6304 | 0.4088 | 0.6722 | 0.5446 |
| 6 | 0.5542 | 0.7574 | 0.4248 | 0.6446 | 0.5952 |
| 7 | 1.0000 | 0.3333 | 0.4248 | 1.0000 | 0.6895 |
| 8 | 0.4755 | 0.6847 | 0.3714 | 0.5150 | 0.5117 |
| 9 | 0.6660 | 0.4270 | 0.3333 | 0.5989 | 0.5063 |
| 10 | 0.4375 | 0.6788 | 0.4248 | 0.6722 | 0.5533 |
| 11 | 0.4108 | 0.6020 | 0.3514 | 0.6357 | 0.5000 |
| 12 | 0.3795 | 0.4969 | 0.4362 | 0.5949 | 0.4769 |
| 13 | 0.7959 | 0.5217 | 0.4610 | 0.6802 | 0.6147 |
| 14 | 0.4691 | 0.5826 | 0.4483 | 0.5196 | 0.5049 |
| 15 | 0.4295 | 0.6428 | 0.3476 | 0.6188 | 0.5097 |
| 16 | 0.6314 | 0.5526 | 0.5039 | 0.4927 | 0.5451 |
| 17 | 0.5585 | 0.4146 | 0.3892 | 0.3333 | 0.4239 |
| 18 | 0.7997 | 0.5826 | 0.5372 | 0.3769 | 0.5741 |

assessment of the multiple objective optimization determined using Eq. (5).

$$\gamma_{j} = \frac{1}{b} \sum_{a=1}^{b} \chi_{i}(a), \qquad (5)$$

where γ_j is the GRG of *j*th experiment and *b* is the number of performance characteristics.

3 DISCUSSION

The multi-response performance index presented in Table 6 presents the average value of the GRG for every level. The highest value of GRG indicates the best possible level of the process parameters. The calculated higher GRG value indicates the closeness to the optimal value. The total mean of the GRG for the eighteen runs was estimated and is presented in Table 6. The optimal parameter combination for better MR and lesser TWR, OC and TO is found to be $(A_1B_1C_3D_1)$ as given in Table 6.

Table 6. Multi response performance index

| Symbol | Level 1 | Level 2 | Level 3 | Main effect (max-min) | | | |
|------------------|---------|---------|---------|-----------------------|--|--|--|
| А | 0.5738 | 0.5598 | 0.5418 | 0.0321 | | | |
| В | 0.6148 | 0.4958 | 0.5648 | 0.1191 | | | |
| С | 0.5377 | 0.5649 | 0.5728 | 0.0351 | | | |
| D | 0.5934 | 0.5204 | 0.5615 | 0.0730 | | | |
| $y_i = = 0.5585$ | | | | | | | |

3.1 ANOVA

The influence of process parameter on the performance characteristic was analyzed using analysis of variance (ANOVA). The effect of process parameters is measured by the sum of the squared deviations. It predicts" the influential process parameter on output performance. The total sum of the squared deviations (SS_D) from the total mean of the GRG y_i can be calculated as:

$$SS_D = \sum_{j=1}^p (\gamma_{j-}\gamma_i)^2.$$
(6)

In which, *p* is the number of experiments in the OA and γ_j is the mean of the GRG for the *j*th experiment.

The sum of the squares (SS) calculated is divided by degrees of freedom (DoF) to obtain mean square of a factor (MS_j) or error (MS_e) . The percentage contribution (φ) of each of the design parameters is obtained using the Eq. (7) [14].

$$\varphi_j = \frac{ss_j}{ss_T}.$$
(7)

Moreover, Fisher's test (F test) is also performed to establish machining parameters' influence on the performance characteristic [17]. ANOVA for GRG is presented in Table 7. Based on the ANOVA, table voltage and pulse off-time show a higher percentage contribution, hence voltage and pulse off-time are dominant parameters that affect the MR, TWR, OC and TOC. In EDM, increase voltage increase the current required for machining which improves the ionization effect between the tool and electrode. This ionization effect increases the temperature of the tool and electrode, resulting in melting of workpiece material. The molten material resulted from heating is evaporated during pulse off time of the EDM process. Hence, the voltage and pulse off-time are considered as significant factors in EDM.

| Table | 7. | ANOVA | table |
|-------|----|-------|-------|
| | | | |

| Factors | DoF | SS | MSj | F ratio | φ |
|------------------|-----|-------|--------|---------|-----------|
| Ι | 2 | 0.003 | 0.0016 | 0.2931 | 2.72 |
| V | 2 | 0.042 | 0.0214 | 4.056 | 37.71 |
| ton | 2 | 0.004 | 0.002 | 0.3841 | 3.57 |
| t _{off} | 2 | 0.016 | 0.008 | 1.521 | 14.14 |
| Error | 9 | 0.047 | 0.0053 | | 41.84 |
| Total | 17 | 0.113 | 0.0067 | | 100 |

3.2 Confirmation Test

Confirmation tests were performed to show the improvement of performance characteristics [14]. The calculated GRG (I) is calculated as shown below:

$$\eta = \eta_m + \sum_{i=1}^q (\eta_i - \eta_m), \qquad (8)$$

where η_m is the total mean of the GRG, *q* is the number of significant parameters; η_i is the mean of the GRG at the optimal level. The predicted MR, TWR OC and TOC overcut and GRG for the best possible machining factors are estimated using the Eq. (8). Based on the confirmation test, GRG has improved by 0.0153 from the initial level; hence, as a whole, the performance of EDM process has been improved.

3.3 TOPSIS

The TOPSIS method is used to find an ideal solution, and the following steps are followed to find the optimal parameter combination [18]. Step 1: The decision matrix consists of 'n' attributes and 'm' alternatives, and it is represented in Eq. (9).

$$\mathbf{A} = \begin{bmatrix} T_{11} & T_{12} & \dots & T_{1n} \\ T_{21} & T_{22} & \dots & T_{1n} \\ \vdots & \vdots & \ddots & \vdots \\ T_{m1} & T_{m2} & \dots & T_{mn} \end{bmatrix}.$$
 (9)

Here T_{ij} is the performance of *i*th alternative with respect to *j*th attribute.

Step 2: Using Eq. (10), normalize decision matrix values were found.

$$r_{ij} = \frac{T_{ij}}{\sqrt{\sum_{i=1}^{m} T_{ij}^2}}, \quad j = 1, 2, \cdots, n.$$
(10)

Step 3: Weight for each response are calculated, and the associated weights are multiplied with normalized decision matrix to obtain the weighted normalized decision matrix. The weighted normalized decision matrix is obtained as:

$$R_{ij} = M_i \times r_{ij},\tag{11}$$

where i=1,...,m and j=1,...,n. M_j represents the weight of the *j*th attribute or criteria.

Step 4: Positive ideal solution (PIS) and negative ideal solution (NIS) are determined as follows:

$$N^{+}=(n_{1}^{+}, n_{2}^{+}, ..., n_{x}^{+})$$
 maximum values, (12)

$$N^{-}=(n_{1}^{-}, n_{2}^{-}, ..., n_{x}^{-})$$
 minimum values. (13)

Step 5: The separation of each alternative from positive ideal solution (PIS) is calculated as:

$$\alpha_i^+ = \sqrt{\sum_{j=1}^n (T_{ij} - x_j^+)^2}, \quad i = 1, 2, ..., m.$$
 (14)

The separation of alternatives form the negativeideal solution is expressed in Eq. (15).

$$\alpha_i^- = \sqrt{\sum_{j=1}^n (T_{ij} - x_j^-)^2}, \quad i = 1, 2, ..., m.$$
 (15)

Step 6: Eq. (16) is used to find the relative proximity of the different alternative to the ideal solution.

$$P_{i} = \frac{\alpha_{i}^{-}}{\alpha_{i}^{+} + \alpha_{i}^{-}}, \quad i = 1, 2, ..., m.$$
(16)

Step 7: the P_i values (preference value) are ranked in descending order to find the optimal parameters combination.

3.4 TOPSIS Analysis

The four responses such as MR, TWR, OC and TOC are normalized using the Eq. (10). In this analysis, the weight criterion for MR, TWR, OC and TOC are 0.2154, 0.0177, 0.5644 and 0.2026, respectively. The relative normalized weight matrix has been computed using the proper weight criteria. The weight criteria are multiplied to obtain the normalized weighted matrix using Eq. (11). The ideal and the negative ideal solutions are calculated from the normalized weighted matrix table; that is, $V_{MR}^+ = 0.0778$, $V_{MR}^- = 0.0164$, $V_{TWR}^+ = 0.0077$, $V_{TWR}^- = 0.0002$, $V_{OC}^+ = 0.5417$, $V_{OC}^- = 0.2040$, $V_{TOC}^+ = 0.0900$ and $V_{TOC}^- = 0.0121$. The separation measures of each condition from the ideal and negative ideal solutions were computed with Eqs. (14) and (15). Finally, the relative closeness coefficient (CC) value for each combination of factors of EDM process is calculated using Eq. (16), which is shown in Table 8. It is evident from Table 1 that experiment No. 1 is the best experiment and experiment No. 3 is second best alternative. According to this result, it is recommended to choose experiment No. 1, which has the highest proximity coefficient value among alternative experiments. Thus, it is evident from the TOPSIS analysis that the combination of process parameters such as 10 A, 30 V, 100 µs and 20 µs is suitable for the best EDM performance measures.

On comparing the grey-Taguchi and TOPSIS method results, the best level for *I*, *V* and t_{off} are 10 A, 30 V and 20 µs. Based on these results, the pulse on time shows two optimal levels, 100 µs and 200 µs, respectively. Although the levels for pulse on time are different, it will not have any significant impact on the performance since the contribution of pulse on time is very minimal, as shown in ANOVA Table 7. Hence, based on the results, it is clear that both these approaches are viable for arriving at the optimal process parameter combination with the available sparse data.

3.5 Analysis of Tool Wear

The tool electrode is the important factor which decides the shape accuracy of the drilled hole. In order to understand the tool wear behaviour, experiments are conducted by varying one parameter at a time. Based on Table 7, the voltage is the most influential parameters. Hence, the voltage is varied by keeping

| Experiment | | Normali | zed data | | | Weighted no | rmalized data | a | Separatior | measures | Closeness coefficient |
|------------|--------|---------|----------|--------|--------|-------------|---------------|--------|--------------|--------------|-----------------------|
| No. | MR | TWR | OC | TOC | MR | TWR | OC | тос | α_i^+ | α_i^- | Pi |
| 1 | 0.0759 | 0.0104 | 0.9598 | 0.1920 | 0.0164 | 0.0002 | 0.5417 | 0.0389 | 0.0802 | 0.3644 | 0.8196 |
| 2 | 0.1696 | 0.2235 | 0.6467 | 0.2764 | 0.0365 | 0.0039 | 0.3650 | 0.0560 | 0.1846 | 0.2062 | 0.5276 |
| 3 | 0.2605 | 0.0983 | 0.7848 | 0.1470 | 0.0561 | 0.0017 | 0.4429 | 0.0298 | 0.1178 | 0.2599 | 0.6881 |
| 4 | 0.2245 | 0.1684 | 0.7479 | 0.2138 | 0.0484 | 0.0030 | 0.4221 | 0.0433 | 0.1318 | 0.2516 | 0.6563 |
| 5 | 0.1983 | 0.1967 | 0.5269 | 0.1536 | 0.0427 | 0.0035 | 0.2974 | 0.0311 | 0.2538 | 0.1161 | 0.3138 |
| 6 | 0.2463 | 0.1521 | 0.5547 | 0.1658 | 0.0531 | 0.0027 | 0.3130 | 0.0336 | 0.2368 | 0.1365 | 0.3657 |
| 7 | 0.3610 | 0.4341 | 0.5547 | 0.0598 | 0.0778 | 0.0077 | 0.3130 | 0.0121 | 0.2415 | 0.1254 | 0.3417 |
| 8 | 0.2038 | 0.1756 | 0.4535 | 0.2408 | 0.0439 | 0.0031 | 0.2559 | 0.0488 | 0.2907 | 0.0955 | 0.2473 |
| 9 | 0.2895 | 0.3238 | 0.3614 | 0.1885 | 0.0624 | 0.0057 | 0.2040 | 0.0382 | 0.3420 | 0.0724 | 0.1747 |
| 10 | 0.1777 | 0.1780 | 0.5547 | 0.1536 | 0.0383 | 0.0031 | 0.3130 | 0.0311 | 0.2394 | 0.1303 | 0.3524 |
| 11 | 0.1565 | 0.2091 | 0.4075 | 0.1700 | 0.0337 | 0.0037 | 0.2300 | 0.0344 | 0.3197 | 0.0537 | 0.1439 |
| 12 | 0.1279 | 0.2681 | 0.5729 | 0.1907 | 0.0276 | 0.0047 | 0.3233 | 0.0386 | 0.2299 | 0.1465 | 0.3892 |
| 13 | 0.3244 | 0.2523 | 0.6098 | 0.1502 | 0.0699 | 0.0045 | 0.3442 | 0.0304 | 0.2065 | 0.1684 | 0.4493 |
| 14 | 0.1997 | 0.2187 | 0.5916 | 0.2375 | 0.0430 | 0.0039 | 0.3339 | 0.0481 | 0.2148 | 0.1686 | 0.4397 |
| 15 | 0.1717 | 0.1914 | 0.3979 | 0.1783 | 0.0370 | 0.0034 | 0.2246 | 0.0361 | 0.3242 | 0.0533 | 0.1412 |
| 16 | 0.2778 | 0.2341 | 0.6650 | 0.2578 | 0.0598 | 0.0041 | 0.3753 | 0.0522 | 0.1716 | 0.2169 | 0.5583 |
| 17 | 0.2483 | 0.3353 | 0.4900 | 0.4442 | 0.0535 | 0.0059 | 0.2765 | 0.0900 | 0.2662 | 0.1596 | 0.3747 |
| 18 | 0.3253 | 0.2187 | 0.7019 | 0.3776 | 0.0701 | 0.0039 | 0.3961 | 0.0765 | 0.1464 | 0.2639 | 0.6431 |

Table 8. Normalized data, weighted normalized data, separation measures and closeness coefficient values



Fig. 2. SEM micrographs; a) 30 V, 14 A, 200 µs and 40 µs, b) 40 V, 14 A, 200 µs and 40 µs, c) 50 V, 14 A, 200 µs and 40 µs

the other parameters such *I*, t_{on} , and t_{off} constant. The voltage value is varied as 30 V, 40 V, 50 V by keeping the *I*, t_{on} , and t_{off} at 14 A, 200 µs, and 40 µs, respectively. Each experiment is repeated once. Based on the SEM micrograph, which is shown in Fig. 2, it is evident that the wear pattern varies with the voltage. It is evident from Fig. 2 that the recast layer pattern observed around the circumference of the hole varies with voltage. It is due to the fact that tool wear on the electrode is not even and, hence, the uneven electrode face will have different proximity towards the workface, resulting in uneven recast layer on the circumference of the hole. Further studies are required to understand the tool wear behaviour when machining Inconel 718.

4 CONCLUSIONS

Machining characteristic optimization of EDM for Inconel 718 is preformed using grey-Taguchi method. The optimal machining parameters were found using GRG for multi-performance characteristics. Eighteen experimental runs based on OA have been performed. The optimal combination of input parameter to acquire better responses based on grey-Taguchi has been found to be I (10 A), V (30 V), t_{on} (200 µs) and t_{off} (20 µs). According to ANOVA, the voltage and t_{off} plays a prominent role in machining Inconel 718. The confirmation test result proves that there is a notable improvement in the GRA value from 0.6969 to 0.7122, when machining is done with the optimal parametric combination. Based on the confirmation test, it is evident that GRA may be applied with sparse data in manufacturing industries to optimize the EDM process parameters to be competitive in the market. The best combinations identified using the TOPSIS method for better performance measures is 10 A, 30 V, 100 μ s and 20 μ s. These multi-objective optimization techniques are found to be suitable for optimizing the EDM process parameter. Tool wear behaviour is also studied through SEM images by varying the voltage. The SEM micrographs confirm that the wear pattern varies with the voltage. Hence detail analysis and optimization of electrical parameters may be considered as future work.

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